Managing Learning Through Mathematical Literacy Based on Cognitive Load

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Abstract: The object of mind is something that must be taught by the teacher to the student in the form of learning, or we know that the teaching is the process of interaction between students, between students and teachers, and learning resources in the learning environment so that with it we as educators need to optimize the student's thought process so that students can be optimal for information. There are three sources of how students obtain optimization in the learning process, namely: intrinsic cognitive load (depending on the difficulty level of material), extraneous cognitive load (depending on the presentation of thematerial) and germane cognitive load (which is imposed by teaching methods that lead to better learning outcomes). The results showed that the interactive element is well managed and extraneous cognitive load is suppressed to a mable so that it creates a large enough germane cognitive load.

Keywords: geometry, cognitive load theory

1. Introduction

Mathematics is the science of logic about shapes, arrangements, magnitudes and concepts-other related concepts with large numbers divided into three fields, namely algebra, analysis and geometry, or it can be said that mathematics is abstract ideas given the symbols are arranged hierarchically and reasoning is deductive, so learning mathematics is a high mental activity. Geometry is one of the important aspects of mathematics to learn and requires high mental activities but at the same time difficult for students to understand.

The lack of optimal understanding of students on geometry is evidenced by the national examination (UN) of junior high school students in Indonesia which shows that overall students are only able to answer the correct questions at most. With material details of the group numbers 39.71%, algebra 51.24%, geometry 42.27% and statistics and odds of 55.60%. for West Java province, UN scores numbered 39.67%, algebra 52.69%, geometry 42.98% and statistics and opportunities by 56.12% (PUSPENDIK, 2019), whereas this field of geometry is a field that must be studied by students in accordance with the curriculum 2013.

There are three reasons why geometry is studied. First, "geometry uniquely connects mathematics with the real physical word." Geometry associates mathematics with physical forms in the real world. For example, a beehive that is a representation of the sixth hexagonal arrangement. Second, "geometry uniquely enables ideas from other areas of mathematics to be pictured." Geometry allows other mathematical ideas to be visualized. For example, solving statistical problems using bar charts, pie charts, or various curves. The third "geometry nonuniquely provides an example of a mathematical system." In general geometry provides an example of a mathematical system, such as proving two parallel lines using a basic theorem of support.

The description above explains that matematika learn about order, about organized structures, mathematical concepts arranged hierarchically, structured and systematic, ranging from the simplest concepts to the most complex concepts. In mathematics the basic object studied is abstrak, so called a mental object, it is an object of thought.

The object of the mind is something that must be taught by the teacher to the student in the form of learning, or we know that the teaching is the process of interaction between students, between students and teachers, and learning resources in the learning environment (Per mendikbud No. 103 Year 2014). In a learning environment that is the main goal is to makentu students to be able to learn. Learning is the process of changing the composition of knowledge that has been stored in memory through the reconstruction of old knowledge and constructing new knowledge. Knowledge reconstruction is usually done by thinking process.

The thought process according to Atkinson and Shiffrin (Glassman & Hadad, 2009) there are two ways for students to think, namely by perception and encoding. Perception reinterpretation of information received using the senses and subsequent interpretation can be included in long-term memory through the working memory of our brain or we call encoding. But sometimes there are differences in the demands of the task or material that must be mastered by one's ability to master the demands, especially for mathematical concepts that precurs the precuring of certain material to understand it. This is known as cognitive load theory. It can be said that this theory of cognitive load is a psychological theory that explains the amount of burden that occurs in human cognitive due to tasks that exceed its capacity. Cognitive load includes three sources, namely: intrinsic cognitive load, extraneous cognitive load, and germane cognitive load (Plass, J.L., et al, 2010).

Intrinsic cognitive load depends on the difficulty level of a material, but with good presentation techniques and does not complicate the understanding of learners it will be managed intrinsic cognitive load. Extraneous
cognitive load depends on the presentation of the material. Whereas germane cognitive load is a relevant or beneficial burden imposed by teaching methods that lead to better learning outcomes. In learning, cognitive overload depends on the degree of difficulty of the material studied according to intrinsic cognitive load. If the material studied intrinsic cognitive load is high, then the learning design must be organized in such a way that extraneous cognitive load can be pressed to a maximum. This is in line with previous studies that stated that the process of defense ran based on cognitive load theory is able to solve mathematical problems (Damayanti, 2013; Fitriyah, et al., 2014; Kristiana, 2015).

The process of managing cognitive load can go through the mathematical literacy process, because the indicators of the domain of the mathematical literacy process include formulating the situation mathematically, using mathematical concepts, facts, procedures and reasoning and interpreting, applying and evaluating mathematical results (OECD, 2017) and this is very relevant to geometry material. Based on the description that has been explained, this paper will describe how to manage mathematics learning based on students’ cognitive load, with the objectives of research as follows: 1). describe cognitive load theory; 2). how to manage learning through mathematical literacy based on cognitive load theory on geometry material.

2. Methodology

Research Design
This research uses qualitative approach. Qualitative approaches are used because the study tries to describe and express, excavate and find broad points of view regarding students’ cognitive load (Johnson and Christensen, 2004). the type of research used is descriptive research. This descriptive study tries to illustrate how cognitive burdens are in geometry learning (Creswell, 2009).

Population and Sample
The population in this study was all students of SMPNegeri 2Ciampel Karawang Regency in class VII, with the sample of the research being one class on geometry material in class VII with reference to the 2013 curriculum. geometry coverage in junior high school students in class VII is triangular and quadrilateral.

Data Collection
Instruments or supporting tools in this research are articles on the theory of cognitive load, the domain of mathematical literacy process issued by the OECD, KI and KD grade VII as a reference, geometry material at the junior high school level grade VII with triangular and quadrilateral materials and interview guidelines. Researchers in this study acted as the main instrument as well as data collectors, the observed learning is a learning activity carried out by math teachers as usual without any engineering or regulation. This activity is carried out so that the results obtained really illustrate the cognitive burden in learning geometry materials and how efforts to manage cognitive load through mathematical literacy process.

Data Analysis
The data analysts are in through several steps. The steps in this study include: preparation (completeness of instruments), domain analysis of mathematical literacy process and cognitive load components, data collection (observation and interview), data processing, and report writing. All instruments analyzed by researchers to be able to answer questions so that the final results are expected to provide examples of geometric teaching materials design through a mathematical literacy process based on cognitive load.

3. Results & Discussion
Based on the purpose of the research mentioned, the authors tried to discuss one by one, starting from the description of the theory of cognitive load and how the efforts to manage the theory of cognitive load in mathematics learning with geometric materials and the impact of the application of this theory to geometry learning.

Cognitive Load Theory
Cognitive load theory is a psychological theory that tries to explain that there is a difference in demands between the task and the ability of a person to master these demands so that here it is explained how our working memory efforts in processing information / tasks given at one time so that learning outcomes can be predicted (Moray, 1979; Cooper, 1990; Plass., Moreno., Sweller, 2010). So there is a basic, cognitive load theory asserting that learning can be hampered when working memory capacity is exceeded in learning tasks.

Working memory works for the thought process. Berpikir is one of the abilities that teachers should teach students. One theory that discusses how human thought processes were put forward by Atkinson and Shiffrin in 1968 (Glassman&Hadad, 2009). These two cognitive psychology experts managed to explain how human
thinking devices and processes that occur clearly, logically and simply. Their theories are both known as information processing theories.

![Atkinson and Shiffrin Information Processing Theory Model](image)

**Figure 1: Atkinson and Shiffrin Information Processing Theory Model**

Speaking of a general thought process, there are many things involved in that process from the beginning. Among them is the role of memory or memory as well as information sharing. It should be necessary to know the concept of memory model and information processing in order to further analyze a thought process. Before exploring more about these two things, it is necessary to introduce first the concept that is also related to both. That is, the concept of perception. Suharnan (2005) mentions perception is a process of using knowledge that has been possessed (stored in memory) to detect or obtain and interpret the stimulus received by sensory devices such as, eyes, ears and nose. Based on this understanding, it can be said that perception is the process of interpreting information received using a sense tool.

There are 3 relevant aspects in perception related to human cognition, namely, the recording of the senses, pattern recognition and attention. The first aspect, the recording of the senses is a memory system designed to store a record of the information received by receptor cells. Sensory recording is also known as sensory memory that is distinguished into two kinds, namely, iconic sensory recording system against visual information, images and concrete and echonic objects that is the sensory recording system against information in the form of sound.

The second aspect, pattern recognition is the process of transformation and organizing information that is still abusive in order to have a certain meaning or meaning. This aspect is deeper than just storing the information entered through receptors, in other words it can also be said that the aspect of pattern recognition is an effort to organize incoming information in accordance with the characteristics that stand out to be placed according to the type.

Attention is the third aspect, which is defined as the process of centralizing mental activity or the process of concentration of the mind by ignoring other unrelated stimuli. This activity requires concentrating the concentration of the mind on the things that stand out from an information and works intensely on the information by ignoring the uncons relates.

The initial receiver of information on this sense is referred to as sensory memory. According to the study, information from vision can only last less than a second in sensory memory, while information from hearing can last three to four seconds. If attention is not paid to such information then they will be lost. But if attention is given then the information will be forwarded to short-term memory which can retain information from 15 seconds to 30 seconds (Driscoll, 2005). Information will be lost if we do not repeat the attention to him. However, if a repeat is performed then the information can be passed on to long-term memory.

The researchers state that long-term memory can store information for a very long time, depending on its use as revealed by Baddeley (2012) mentioning working memory is responsible for processing information and following up on such information. If the technique for passing information on to long-term memory is through repetition, we call it the process of memorizing or remembering.

The second way to pass on information to long-term memory is to understand (encoding). The point is to connect the new information with the various old information that we have (stored in the previous long-term memory). This second way is believed to make information more durable in our memory. In addition, by understanding then all the information will be more useful in the application of daily life.

Various information stored in long-term memory, can at any time be called by short-term memory if we need it (for example when facing certain problems). Miller (Nurist, 2015) says working memory can only store about seven items or pieces of information at a time. When processing information (organizing, showing differences, and comparing), humans can manage only two or three items of information simultaneously, depending on the type of processing required (Kirschner, Sweller, & Clark, 2006). Until now experts have not been able to determine exactly what human long-term memory storage capacity is. It is therefore said that our long-term memory capacity is unlimited.

Based on the description above it is clear that the theory of cognitive load is trying to optimize the tasks that come in on long-term memory so that learning can be optimal. Cognitive load theory can be caused by three sources, namely: intrinsic cognitive load, extraneous cognitive load, and germane cognitive load (de Jong, 2009; Plass, J.L., et al., 2010; Sweller, 2010). Intrinsic cognitive load is related to the inherent characteristics of the
Managing Learning Through Mathematical Literacy Based on Cognitive Load

Intrinsic cognitive load in learning is caused by two things namely, element interactivity and elements isolated / interacting element (Artino, 2008). The second is extraneous cognitive load is a load caused by instructional materials used to present content, and germane cognitive load refersto the load imposed by the learning process.

In other words intrinsic cognitive loads and extraneous cognitive loads are cognitive loads associated with elements of interactivity in learning whereas cognitive loads are cognitive burdens associated with mental effort relevant to understanding. Intrinsic cognitive loads and extraneous cognitive loads tend to interfere in learning whereas cognitive loads tend to be supportive in learning (Lin and Lin, 2013). High extraneous cognitive load in learning results in poor student performance while germane high cognitive load results in better student performance (Jong, 2010).

Based on the exposure of cognitive load theory, it can be concluded that the cognitive load of students contains three types of cognitive processing during learning, namely:

1. **Intrinsic cognitive load** is a burden of thought experienced by students during learning due to the demands of content.
2. **Germane cognitive load** is a burden of thought experienced by students during learning caused by the need to integrate new information with previous knowledge.
3. **Extraneous cognitive load** is a burden of thought experienced by students during learning caused by the work of the mind that is not in accordance with the objectives of learning (Clark et al, 2006).

Managing Learning Through Mathematical Literacy Based on Cognitive Load

To be able to see how to manage learning through mathematical literacy based on cognitive load, especially geometry material in grade VII with triangular and quadrilateral concepts, then the analysis of the domain cognitive load and indicators domain literacy process, observation on the learning process and interviews in students so that it can conclude how efforts to manage the learning. Here are some steps from the research done:

1. **Mathematical literacy and cognitive load domain analysis based on sources and interviews and observations**

   **Mathematical literacy**

   Domain mathematical literacy process which is divided into three indicators with a range of different activities on each indicator. Here are three indicators of the process domain and the activities in each of its indicators, in table 1:

   **Table 1. Mathematical Literacy Process Domain Indicators**

<table>
<thead>
<tr>
<th>Indicator</th>
<th>Activities</th>
</tr>
</thead>
<tbody>
<tr>
<td>Formulating the situation</td>
<td>1. Identify mathematical aspects of problems that lie in real-world contexts and identify significant variables.</td>
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<tr>
<td>Formulating the situation</td>
<td>2. Recognize mathematical structures (including regularity,</td>
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<tr>
<td>mathematically.</td>
<td>relationships and patterns) in problems or situations.</td>
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<td></td>
<td>3. Simplify a situation or problem to make it accept mathematical</td>
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<td></td>
<td>analysis.</td>
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<td></td>
<td>4. Identify the constraints and assumptions behind mathematical</td>
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<td>modeling and simplifications collected from context.</td>
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<td></td>
<td>5. Represent the situation mathematically, using appropriate variables,</td>
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<td>symbols, diagrams and standard models.</td>
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<td></td>
<td>6. Represent the problem in different ways, including arranging it</td>
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<td>according to mathematical concepts and making precise assumptions.</td>
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<td></td>
<td>7. Understand and explain the relationship between the specific language of</td>
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<td>the problem context and the symbolic and formal language needed to</td>
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<td></td>
<td>mathematically represent it.</td>
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<td></td>
<td>8. Translate the problem into a mathematical or representational language.</td>
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<td>9. Identify aspects of the problem that correspond to known problems or</td>
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<td>mathematical concepts, facts or procedures.</td>
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<td></td>
<td>10. Use technology (such as spreadsheets or list facilities on graphing</td>
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<td>calculators) to describe mathematical relationships inherent in contextual</td>
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<td>problems.</td>
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</table>

   In addition to the activities listed above, the following measures have been added to PISA-D.
<table>
<thead>
<tr>
<th>Indicator</th>
<th>Activities</th>
</tr>
</thead>
</table>
| Using mathematical concepts, facts, procedures, and reasoning            | 1) Selecting the appropriate model from the list.  
2. Designing and implementing strategies to find mathematical solutions.  
3. Use mathematical tools, including technology, to help find the right solution or forecast.  
4. Apply facts, rules, algorithms and mathematical structures when searching for solutions.  
5. Manipulating numbers, graphical and statistical data and information, algebraic expressions and equations, and geometric representations.  
6. Make mathematical diagrams, graphs and constructions and extract mathematical information from them.  
7. Use and switch between different representations in the process of finding a solution.  
8. Make generalizations based on the results of applying mathematical procedures to find solutions.  
9. Reflect mathematical arguments and explain and justify mathematical results.  

In addition to the activities listed above, the following activities have been added to PISA-D:  
1) Do a simple calculation.  
2) Draw simple conclusions.  
3) Choose the right strategy from the list.  

| Interpret, apply and evaluate mathematical results.                      | 1. Interpret mathematical results back into a real-world context.  
2. Evaluate the fairness of mathematical solutions in the context of real-world problems.  
3. Understand how the real world affects the results and calculations of mathematical procedures or models to make contextual assessments of how results should be adjusted or applied.  
4. Explain why mathematical results or conclusions, or not, make no sense given the context of the problem.  
5. Understand the level and limits of mathematical concepts and mathematical solutions.  
6. Criticize and identify the boundaries of the model used to solve a problem.  

In addition to the activities listed above, the following measures have been added to PISA-D:  
1) evaluate mathematical results in context.  

(OECD, 2017)

**Cognitive Load Theory**  
Consists of three components, namely:

**Intrinsic cognitive load**  
Intrinsic cognitive load is determined by the degree of complexity or difficulty of the material being studied (Sweller & Chandler, 1994). Intrinsic cognitive load cannot be manipulated because it is already a character of interactive elements in a material, so it is fixed (constant) (Sweller, et al. 2011). Material that intrinsically has a heavy load, if presented properly, then the cognitive processes in working memory will be able to run smoothly. Conversely, although the intrinsic load on a material is light, but if the presentation is not good, then the cognitive processes of students in working memory will run slowly or stop working.  

Intrinsic cognitive load, determined by the level of complexity of the information or material being studied. An important factor in teaching a material is understanding the emergence of interactivity elements, namely a number of elements that must be jointly processed in working memory under instructions. The element of interactivity is fixed because it is intrinsically possessed by all the material that must be studied and cannot be changed. This element appears in learning caused by elements that must be processed simultaneously between elements in the material or in other words determined by the interaction between important elements of
information used to understand the material (Kalyuga, 2011).

Based on the observation and interview of interactivity elements in geometry learning is related to the difficulty of imagining how to determine the position of a point, line, and field. Students must be able to represent and interpret the position of a point, line, and field so that then the student is able to determine the distance from the point, line, and field. Students in learning geometry do have difficulty in imagining. The difficulty of imagining resulted in students being less able to configure in terms of point of view, introduction of form and position, and representation from a point of view (Gal and Linchevski, 2010).

**Extraneous cognitive load**

Unlike intrinsic cognitive load, extraneous load can be manipulated. Extraneous cognitive load is determined by the technique of presenting the material (Sweller & Chandler, 1994). So this extrinsic burden is related to how to interpret a material in a learning. A good way of presenting the material, namely if the delivery is systematic, practical, effective and interesting. Systematic here means that the material is delivered according to the basic competencies (KD) that exist and in the correct order so that students can connect the material with each other well. Practical is a matter to be considered in the delivery of materials, the practical purpose here the material is delivered neatly, appropriately, and not excessively. Effective in this case has the understanding that the presentation of material must be tailored to the objectives to be achieved in learning. While interesting means that the presentation of the material is done by methods that make students happy, and motivated to follow the learning, for example the presentation is done by displaying with images, colors, and sound audio so that it makes students feel more interested in the material.

Extraneous cognitive load is determined by material presentation techniques and things related to factors that must be minimized in learning, such as the use of confusing teaching materials, noise, and the appearance of computer media that is too much animation.

Extraneous cognitive load in geometry material learning is also caused by some students who are rowdy or crowded. Rowdy or crowded students are students who do not pay attention as the teacher explains. The rowdy or crowded classroom situation is a result of the instructional design of the teacher who does not include the entire student. The teacher's learning is dominant only in some students (tending to be diligent and obedient students) so that some students will be crowded and rowdy themselves. This situation is also called a split-attention situation (Kalyuga, 2011). Students who pay attention to learning will share their attention between listening to the teacher's explanation and the noise caused by some students. So that the crowded learning conditions must be suppressed as low as possible so that students can focus their attention on learning. The extraneous cognitive burden in learning should be suppressed as low as possible (Gerven, Paas, et al., 2002).

Extraneous cognitive load in this study can be seen from the results of interviews that mention that some students, especially those who sit not too in front, sometimes feel disturbed by rowdy students, always nice to chat with their classmates so that sometimes the attention to focus on the material is split, plus sometimes the teacher's voice is less audible for students who feel sitting in the back and there are some parts of the teacher's explanation that are too quick.

**Germane cognitive load**

Germane cognitive load is a cognitive burden caused by cognitive processes that relevant with the understanding of the material being studied. Germane cognitive load means that the memory of students can not organize, construct, codify, elaborate or integrate the material being studied as well-stored knowledge in long-term memory. Germane cognitive load is a relevant or beneficial burden imposed by teaching methods that lead to better learning outcomes. In other words, germane cognitive load can be an effort to build schemes and automation in learning. Germane cognitive load is a burden caused by students' efforts to process and understand the material (Sweller, Ayres, and Kalyuga, 2011). Therefore, in the learning process, germane cognitive load must be improved and to be more effective it needs facilities to bridge the learning (Jong, 2010; Lin and Lin, 2013).

Germane cognitive load in geometry material learning is caused by the teacher's efforts when explaining using the help of the Cabri 3D application program. The use of Cabri 3D application program aims to make it easier for students to understand the position of points, lines, and fields in building space. The use of computer programs relevant to the delivery of materials related to point, line, and field position makes it easier for students. The results for germane cognitive load can be seen from the results of interviews that most respondents stated that by using the facilities Cabri 3D, some students stated that students feel able to imagine how the position of points, lines, and fields in building space especially for triangular and quadrilateral fields. Moreover, those who have a visual and auditory type of learning style. As stated (Wardani et al., 2018) that for students with visual and audio learning type will be very effective in the learning process by using facilities (e-learning) in this case specifically Cabri 3D.
2. Syntax that can be used in learning through mathematical literacy based on cognitive load
After the analysis of the mathematical literacy process, then analyze the cognitive load components as well as the data of interviews and observations on mathematics learning. So in the results of the analysis of researchers how the learning process can be done in the classroom through mathematical literacy based on cognitive load on the concept of triangles and quadrilaterals, as described in table 2.

<table>
<thead>
<tr>
<th>Sintak Learning Models</th>
<th>Learning Activities</th>
</tr>
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<tbody>
<tr>
<td>Matematization</td>
<td>1. Identify issues by context</td>
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<td></td>
<td>2. Analyze and make assumptions</td>
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<td></td>
<td>3. Apply modeling</td>
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<td>4. Translate into math language</td>
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<tr>
<td>Application</td>
<td>1. Implementing and designing strategies</td>
</tr>
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<td></td>
<td>2. Applying fact (modeling) or information excavation to construct concepts</td>
</tr>
<tr>
<td></td>
<td>Make generalizations</td>
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<tr>
<td>Meaning and Reflection</td>
<td>1. Re-examine the generalization results</td>
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<td></td>
<td>2. Analysis of whether conclusions can be relevant to the problem</td>
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<td></td>
<td>3. Identify the suitability of the model used to troubleshoot</td>
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<td></td>
<td>4. Reflecting and concluding</td>
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</tbody>
</table>

4. Conclusions
Knowledge of how humans think, making their memories enter into long-term memory so that we can say as a learning process. An understanding of human cognitive architecture in acquiring, processing and storing information as a new knowledge is the basis for explaining why some instructional procedures work while others fail. Cognitive Load Theory emphasizes methods to help students achieve optimal abilities based on how the cognitive system works because working memory has limited capacity in processing a certain amount of information together. The management of learning based on cognitive through mathematical literacy results in a stage of the learning process that can be done in the classroom to optimize the improvement of students' abilities.

This research has not yet come to examine the instructional impact of learning management through mathematical literacy process based on cognitive load, so for follow-up researchers try to conduct effectiveness test to see the impact of learning management through mathematical literacy process based on cognitive load on geometry material, especially triangle and quadrilateral.

References


