

Stopping Power of Electrons and Protons in Polyethylene Terephthalate C₁₀H₈O₄, and Polyurethane C₁₇H₁₆N₂O₄

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Abstract: In this work, the entire protons stopping power has been calculated by using Ziegler formula. The protons' energy range were (10-2 keV to 103 keV). The entire electrons stopping power with using Bethe-Bloch formula was designed, the verve range of electrons as of 10 keV to 105 keV in Polyurethane C₁₇H₁₆N₂O₄, and Polyethylene terephthalate C₁₀H₈O₄ which as a polymeric materials for manufacture the astronaut suit. The results in this research were compared with the values of the E-STAR program for light charged particles (electrons) and the values of the SRIM program for the heavy charged particles (protons), and they showed good compatibility and all the mentioned equations were programmed in MATLAB 2013 language.

Keywords: Stopping power, Electrons and proton, Bethe-Bloch formula, Ziegler formula, MATLAB language, SRIM 2013.

1. Introduction

The cessation of energetic ions in the matter has been a topic for several years. It is of great importance to theoretical and experimental physicists. [1- 3], Bethe [4] and Bloch [5, 6] were the leading hypothetical detectives. The charged units are stopping in the matter. Bohr, in his first articles [1- 3], it is proposed a method intended to stop control depending on the evidence that target atoms are traditional oscillators advanced [4], Bethe performed steady important mechanics analysis and an important eq. to define the discontinuing of fast charged particles which move in a quantified way. "Bloch" built connecting method in the middle of the two. Traditional "Bohr" effect fact method and quantum methodology. Here realized an updated "Bethe" formulation called "Bethe-Bloch equation" [5, 6]. This calculation decreases the "Bohr" formulation in small velocity and the "Bethe" formulation, at great speed. In addition, the Bethe's strengthened Moller [7] and Bethe [8].

Discontinuing model by incorporating relativistic alterations. But, the ideas of "Bohr, and Bethe" can just be true for fast elements. Either way, these two theories are utilized now days with the fast speeds. from another hand, for slow elements, the principle of stopping power reduced issue was further established by "Fermi and Teller" [9]. They preserved board average by way of an allowed electron gas and electric discontinuing power plan that has a relation with speed of the shell [10].

A medium's discontinuing power may be clear as the normal energy loss part knowledgeable by the elements of charge each unit pathway distance in the middle in respect [11, 12]. Two basics consist of stopping power: impacts and energy. The main is the most significant result of the communication among the event units and the nuclear electrons form impact preventing power is commonly utilized for decreasing the average mass dependency (ρ) [12]. Absolute discontinuing power might be derived from (SRIM-2003) [13], which uses the quantum mechanical treatment of ion atom collision to measure stopping power and ion spectrum (10 eV – 2 GeV/amu) in matter (the SRIM manual denotes to the atom movement as a 'ion' and all objective atoms as a 'atom') Ziegler and Biersack [11] offered a complete summary of the measurement.

A medium's stopping power may be definite by means of the typical energy loss unit experienced by the particles of charge in unit pathway length in the intermediate under deliberation. [12, 14] Many physicists have unrushed the energy loss in matter, but the elementary, standard derivation was credited to "Bloch", the one who enhanced Bethe's estimate, thus the "Bethe-Bloch" method. The energy loss rate can be written by $(-dE/dx)$; dE/dx actuality a loss of vigor, is a adverse worth [15].

2. Theory

Bethe-Bloch Formula

Bethe [4] has derived an alternative stopping power formula. In contrast to Bohr, from the point of view of quantum mechanism, "Bethe" derivative a discontinuing power method in situation of a high-speed missile. Classical countenance the stopping plan for a gas target of the free electron could be as follow [16]:

$$S(Z, v) = \left(\frac{Ze\omega_p}{v} \right)^2 \ln \frac{2m_e M_p v^2}{(m_e + M_p)\omega_p \hbar} \quad (1)$$

Someplace v , Ze and M_p indicate the speed, charge, and mass of the projectile. ω_p refersto the classical plasma frequency gained from the relationship $\omega_p = \sqrt{\frac{4\pi ne^2}{m_e}}$ as (n) is the density numberof electrons, m_e is the mass ofelectron . Also, for heavyweightmissile $M_p \gg m_e$ the stopping power in Eq.(1) decreases to :

$$S(Z, v) = \left(\frac{Ze\omega_p}{v}\right)^2 \ln \frac{2m_e v^2}{\omega_p \hbar} \quad (2)$$

Two suppositions have been used in this derivation: the stopping caused from excitation and ionization of target electrons from Coulom. Moreover, Interface is known as part of the first Born approximation. The stopping number L_{Bethe} reads,

$$L_{Bethe} = \sum_j f_j \ln \left(\frac{2m_e v^2}{\hbar\omega_j}\right) \quad (3)$$

Where $\hbar\omega_j$ is the energy that corresponds to the j^{th} excitation of electrons in the target atoms and f_j is the generalized force of the oscillator (GOS). In reality, it is very difficult to measure the j^{th} electronic excitement, instead of that, measuring the average energy of the excitement is possible to do and the excitation energy defines itself :

$$\ln I = \sum_j f_j \ln(\hbar\omega_j) \quad (4)$$

It can be come close to spending widely use scrambling relationship[6]

$$I \approx 10Z_2 eV \quad (5)$$

So as to justice the consistency the two both theories and the theory of Bethe to predicte electronics opping power, the effects of electronic stopping power have been presnted. Stopping power of the proton going over the Si target [17].

Ziegler Formula

To close the difference between the high- and low energy theories, interpolation formulas of various degrees of sophistication were suggested by Varelas and Biersa [18].

$$(S)^{-1} = (S_{LOW})^{-1} + (S_{HIGH})^{-1} \quad (6)$$

or

$$(S)^{-1} = S_{LOW}S_{HIGH}/(S_{LOW} + S_{HIGH}) \quad (7)$$

Where S_{LOW} (low stopping power), with $S_{LOW} = A_1 E^{1/2}$ And S_{HIGH} (high stopping power), with

$$S_{HIGH} = \frac{A_2}{E} \ln \left(1 + \frac{A_3}{E} + EA_4\right) \quad (8)$$

Here A_1, A_2, A_3 and A_4 are fitting constants.

At high energy, the fitting formula eq.(3) asymptotically agrees with eq(1).

In addition, as the Varelas_Biersack formula is even simpler and has the correct asymptotic action at both high and low energy levels, Eq.

In general, (3) is used for fitting approximation curves[18].

3. Results And Discussion

Stopping power was calculated by Ziegler and Bethe formula for the first time the stopping power wascalculated on two different types Polyurethane $C_{17}H_{16}N_2O_4$, and Polyethylene terephthalate $C_{10}H_8O_4$ which as a polymeric materials for manufacture the astronaut suit, and with a proton energy range of(10^{-2} keV to 10^3 keV), the electrons' energy range(10 keV to 10^5 keV).The program has been implemented in a language MATLAB 2013.

Polyurethane

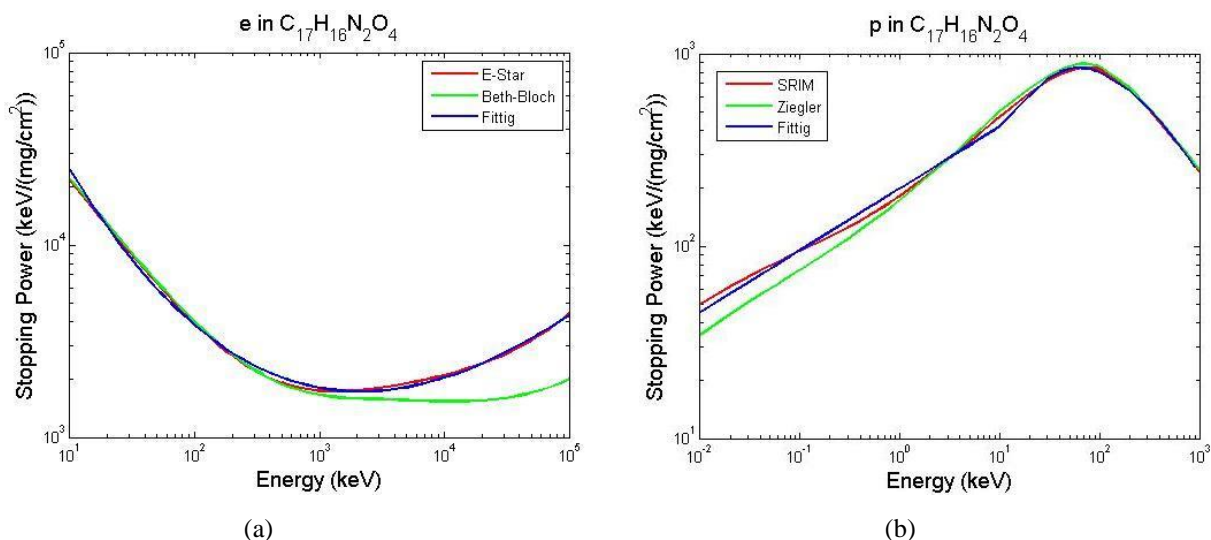


FIGURE 1. Total stopping power (a) forelectrons(b) forprotons in Polyurethane $C_{17}H_{16}N_2O_4$.

Polyethylene Terephthalate

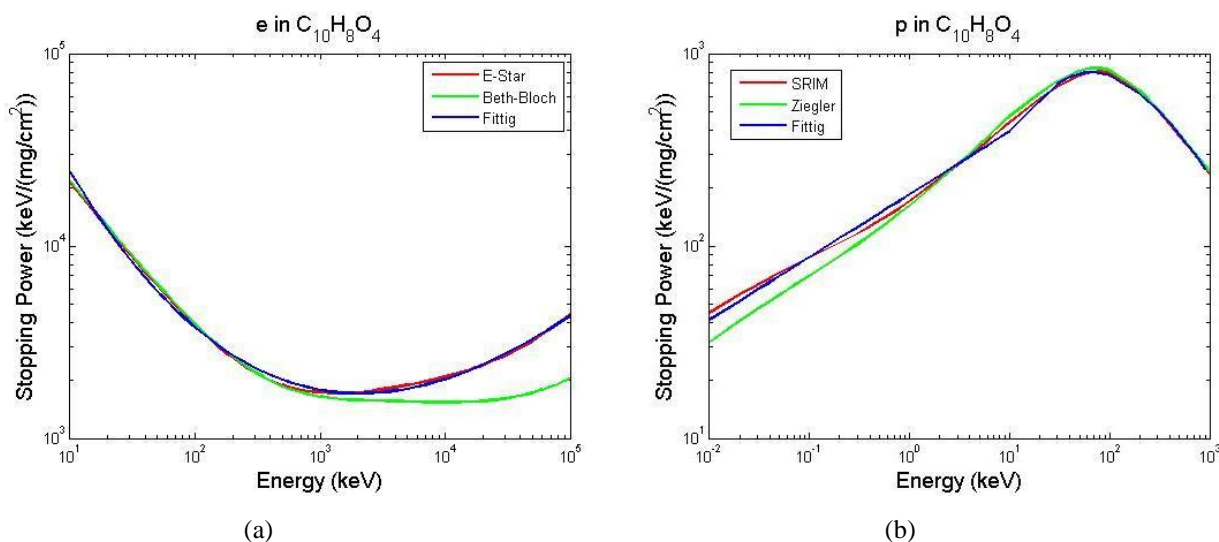


FIGURE 2. Total stopping power (a)forelectrons(b) forprotons inPolyethylene terephthalate $C_{10}H_8O_4$.

TABLE 1.Total stopping power for electron and proton in $C_{10}H_8O_4$ and $C_{17}H_{16}N_2O_4$.

| E (keV) | Total Stopping Power for electron keV/(mg/cm ²) | | E (keV) | Total stopping power for proton keV/(mg/cm ²) | |
|------------|--|----------------------|------------|--|----------------------|
| | $C_{10}H_8O_4$ | $C_{17}H_{16}N_2O_4$ | | $C_{10}H_8O_4$ | $C_{17}H_{16}N_2O_4$ |
| 10 | 21664.05 | 22054.08 | 0.01 | 31.45008 | 34.35136 |
| 100 | 3922.686 | 3982.651 | 0.1 | 69.83289 | 74.98105 |

| | | | | | |
|--------|----------|----------|------|----------|----------|
| 1000 | 1642.979 | 1660.817 | 1 | 162.3784 | 172.8889 |
| 10000 | 1538.956 | 1538.807 | 10 | 470.1188 | 500.9041 |
| 20000 | 1560.986 | 1553.955 | 100 | 816.4049 | 856.6864 |
| 30000 | 1606.453 | 1593.999 | 200 | 640.4915 | 664.3721 |
| 40000 | 1662.16 | 1644.708 | 300 | 514.5034 | 531.0735 |
| 50000 | 1723.245 | 1700.957 | 400 | 434.381 | 447.2909 |
| 60000 | 1787.368 | 1760.353 | 500 | 379.335 | 390.0251 |
| 70000 | 1853.319 | 1821.663 | 600 | 338.7669 | 347.9368 |
| 80000 | 1920.411 | 1884.182 | 800 | 282.0056 | 289.1895 |
| 90000 | 1988.221 | 1947.476 | 900 | 261.0979 | 267.5906 |
| 100000 | 2056.477 | 2011.265 | 1000 | 243.4613 | 249.3883 |

TABLE 2.Rates of elements in C₁₀H₈O₄ and C₁₇H₁₆N₂O₄.

| Polymer | C | H | N | O |
|---|--------|--------|--------|--------|
| C ₁₀ H ₈ O ₄ | 0.6250 | 0.0420 | 0.0000 | 0.3330 |
| C ₁₇ H ₁₆ N ₂ O ₄ | 0.6538 | 0.0516 | 0.0897 | 0.2049 |

TABLE 3.The coefficient of correlation of C₁₀H₈O₄ and C₁₇H₁₆N₂O₄.

| Polymer | For electron | For proton |
|---|--------------|------------|
| C ₁₀ H ₈ O ₄ | 0.9892 | 0.9996 |
| C ₁₇ H ₁₆ N ₂ O ₄ | 0.9895 | 0.9997 |

4. Conclusions

We conclude that the Bethe formula is suitable for the control of the electron stopping power in the studied polymers.

We conclude that the Ziegler formula is suitable for the calculation of the proton stopping power in the studied polymers.

From Figures 1 and 2 banal (a), Calculations indicate that S_{tot} decreases with increasing energy of the incident electrons at the energies (10 - 10³) keV because of the impact discontinuing power is the effect, then the total discontinuing power increases by increasing the energy of in incident electrons at the energies (10³ - 10⁵) keV because the radiative stopping power is effective, and this energy depends on the speed of the electrons that limit the type of interactions with the target and depends on the speed of the electrons that determine the type of interactions with the target.

From Figures 1 and 2 banal (b), we note that the total discontinuing power is increases with increasing energy of the incident protons at the energies (10⁻² - 50) keV due to the occurrence of ionization and irritation of the atoms of the medium, which prevail in energy loss. In the range of energy (10²– 10³) keV, we note that the total discontinuing power is decreases with increasing energy of the incident protons because the electronic shutdown is prevalent.

The results of correlation coefficient (r) is very good at 0.9892, 0.9996, 0.9895, and 0.9997.

By calculating the Bethe-Bloch formula and Ziegler formula to calculate the total stopping power in the studies polymer, it was found that results of the curve match are close to the E-star and SRIM results, respectively

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