

Effect of Hartmann number on Natural Convection of Pleural Effusion

T. Padmavathi*¹ and Dr. S. Senthamil Selvi²

1. Research Scholar, Department of Mathematics, VISTAS, Vels University, Pallavaram, Tamilnadu, India. (pathumyanmar@gmail.com)

2. Research Supervisor, Department of Mathematics, VISTAS, Vels University, Pallavaram, Tamilnadu, India.

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ABSTRACT: The most severe pandemic complications of COVID-19 are mainly caused by large droplet transmission. An initial sign of coronavirus disease is pleural effusion. Droplet transmission of the COVID-19 virus can occur by direct contact with inflamed human beings and indirect touch with surroundings surfaces or with objects used by inflamed person. Present study describes the underlying physics of the pleural fluid deformation in the lung on free convection. Pleural effusion (excess fluid) happens whilst fluid strengthens the area surrounded by the chest wall and lung, the tissue around the lung may become inflamed, this can manifest for plenty distinct speculate, such as pneumonia. The various velocity, temperature, concentration profiles are graphically obtained with increasing and decreasing non-dimensional parameter according to the nature of the pleural fluid.

Key words: COVID-19, Hartmann number, Natural Convection, Pleural fluid, Pleural effusion.

1. INTRODUCTION

In many years droplet ailment transmission has usually been a subject of extensive interest in numerous fields. The transposal of microbes and aggressive microorganism from extinct surfaces by affected men and women is a problem with reference to highly poisonous COVID-19 ailment transportation. The airborne transmittal disorder begins while the infectious delegate which includes the influenza, COVID-19 or SARS viruses are exhaled from an inflamed individual. The procedure of transference is arbitrating with aid of complication go with the flow phenomena, length from air-mucous interplay, during evaporation it acts faster to settled down their big droplet length, it makes circumference pollution to the surfaces. Droplets are smaller than for this reason period evaporate quicker than they reach the position.

The primary function of the respiratory tract is gas exchange. The breathing tract carries extensive variety of micro-organisms. Contaminants of pleural fluid migrate through a respiratory tract. The complete breathing tract is continuously exposed to air, the general public of particles are wiped clean out by means of inhalation, however aspiration and mucosal and haematogenous unfold additionally arise. Individuals with healthy lungs hardly ever have any bacterial or virus contamination as particular surface antigens that adhere to mucosal epithelial cells.

A pleural effusion approach that there is an excess build-up of fluid between human lung and the chest wall. Every of our human lungs are surrounded by using pleura. The pleura is a thin membrane that lines the interior of the chest wall and display screen the lungs. There is generally a slight quantity of fluid among the two layers of pleura occupied. This acts like lubricating oil between the lungs and the chest wall as they circulate whilst we breathe. There are numerous varieties of pleural effusion induced with one-of-a-kind treatment followed by way of Transudative pleural effusion is brought on because of fluid leaking into the pleural area improved stress within the blood vessels, heart failure or a low blood protein. Exudative pleural effusion is as a result of hold up blood vessels or infections, tumours, pneumonia.

The complete quantity of human's pleural liquid in degrees between 0.13–0.27 mL. kg^{-2/3}. As currently decided with the aid of urea mixture in topics go through thoracoscopy for remedy of hydropathic hyperhidrosis, is 0.26 mL. kg⁻¹. The protein awareness in pleural fluid and their ratio during capillary plasma are low, it's already reported that the protein of the pleura permeability ought to be small. Generally, 1,700 cells·mm⁻³ were newly deduct in human normal pleural fluid ranges may vary by (75% macrophages, 23% lymphocytes, and 1% mesothelial cells) [1].

In lots of hospitals lately, the spread of respiration infection from recognised cases of influenza and pneumonia may be avoided with the aid of infection control strategies. These are called 'extra safety'. Warmness and mass switch in MHD flows arises in some of the technological applications. Operating fluids may be either Newtonian or non-Newtonian. Inside the study of natural convection via porous media, the majority of the studies attempt has been committed to the flow resulting from a buoyancy impact of Temperature and Concentration variations. Flows induced with the aid of buoyancy consequences of thermal diffusion is detect often in motion of infections in the human respiration tract. Zahra Ahmadinejad, et al [1] discovered differential diagnosis of affected person under gone through dyspnoea and dry cough referred to lung cancer and treated for

- The density of contaminant pleural fluid isn't always consistent and the temperature between the debris are uniform at some stage in the fluid movement due to buoyancy pressure.
- The gravitational force g , act towards vertical downward direction.
- The contaminant pathogens (COVID-19) are spherical (crown like position), non-undertaking, and equal in length and systematically disbursed in the fluid discharge place.

The Governing Equations are based on the proportion of Momentum, Mass, Energy and Species Concentration as in J. Prakash et al. [11].

Equation of Continuity:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad \text{----- (1)}$$

Navier-stokes Equation:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + \nu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + g \beta (T - T_0) + g \beta^* (C - C_0) - \frac{\nu}{k_1} u - \frac{\sigma B_0^2}{\rho} u \quad \text{--- (2)}$$

First law of thermodynamics Equation:

$$\rho C_p \left(\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right) = k_T \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) + j(T - T_0) \quad \text{----- (3)}$$

Species concentration Equation:

$$\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D \left(\frac{\partial^2 C}{\partial x^2} + \frac{\partial^2 C}{\partial y^2} \right) - K_c (C - C_0) \quad \text{----- (4)}$$

where u and v are the velocity of the fluid particle, ρ known as fluid density, p known as pressure, k_1 known as permeability of the porous medium, g known as gravitational acceleration, β known as volumetric coefficient of thermal expansion, β^* known as volumetric coefficient of concentration expansion, ν known as kinematic viscosity, T known as temperature of the fluid, T_0 known as initial temperature, C_p known as Specific heat of the fluid at constant pressure, k_T known as Thermal conductivity of the fluid, j known as Heat absorption, C known as Concentration of the fluid, D known as coefficient of Mass diffusivity of the fluid, K_c known as Chemical Reaction Parameter.

The appropriate initial and boundary conditions under the assumptions, for Velocity involving moving fluid, Temperature and Concentration fields are defined as

$$\text{When } t = 0, \quad u = v = 0, T = T_0, C = C_0, \quad \text{----- (5)}$$

$$\text{When } y = 0, \quad u = v = 0, T = T_w + \epsilon e^{(\lambda t)} (T_w - T_0), C = C_w + \epsilon e^{(\lambda t)} (C_w - C_0) \quad \text{----- (6)}$$

$$\text{When } y = 1, \quad u = 1 + \epsilon e^{(\lambda t)}, T_w = T_0, C_w = C_0 \quad \text{----- (7)}$$

Given problem by way of replacing the subsequent dimensionless quantities to reduce the many unknown dimensional,

$$\tilde{u} = \frac{u}{v_0}; \tilde{v} = \frac{v}{v_0}; \tilde{x} = \frac{x v_0}{\nu}; \tilde{y} = \frac{y v_0}{\nu};$$

$$\tilde{\theta} = \frac{T - T_0}{T_w - T_0}; \tilde{\phi} = \frac{C - C_0}{C_w - C_0}; \tilde{t} = \frac{t v_0^2}{\nu}; \tilde{p} = \frac{p}{\rho v_0^2} \quad \text{----- (8)}$$

where, ϕ and θ are corresponding non-dimensional concentration and temperature respectively.

which implies $\mathbf{v} = \mathbf{v}_0 (1 + \epsilon e^{(\lambda t)})$, where $\mathbf{v}_0$ is a real positive constant additionally considered as the distinctive velocity order 1. Hence the fluid flow is two dimensional, in order to indeterminate length of the fluid region it clears that all of the physical quantities are independent of x -axis. (i.e.,) $\frac{\partial u}{\partial x} = 0$

After applying non-dimensional variables in basic governing Equations (1) to (4), neglecting the (ϵ) symbol produce the equations are,

$$\frac{\partial v}{\partial y} = 0 \quad \text{----- (9)}$$

$$\frac{\partial u}{\partial t} + \frac{\partial u}{\partial y} = -\frac{\partial p}{\partial x} + \left(\frac{\partial^2 u}{\partial y^2} \right) + Gr \theta + Gc \phi - \sigma^* u - H_a^2 u \quad \text{----- (10)}$$

$$\frac{\partial \theta}{\partial t} + \frac{\partial \theta}{\partial y} = \frac{1}{Pr} \left(\frac{\partial^2 \theta}{\partial y^2} \right) + J \theta \quad \text{----- (11)}$$

$$\frac{\partial \phi}{\partial t} + \frac{\partial \phi}{\partial y} = \frac{1}{Sc} \left(\frac{\partial^2 \phi}{\partial y^2} \right) - K \phi \quad \text{----- (12)}$$

The initial & boundary condition making use of non-dimensional quantities becomes,

$$\left. \begin{aligned} \text{When } t = 0, \quad u = \phi = \theta = 0, \\ \text{When } y = 0, \quad u = 0, \theta = \phi = 1 + \epsilon e^{(\lambda t)} \\ \text{When } y = 1, \quad u = 1 + \epsilon e^{(\lambda t)}, \theta = \phi = 0 \\ \text{Where,} \end{aligned} \right\} \quad \text{----- (13)}$$

$$\begin{aligned} Gr &= \frac{g\beta v(T_w - T_0)}{v_0^3} \text{ [GrashofNumber]} & ; Gc &= \frac{g\beta^* v(C_w - C_0)}{v_0^3} \text{ [SolutalGrashofNumber]} \\ \sigma^* &= \frac{v}{v_0 \sqrt{k_1}} \text{ [Porosity Parameter]} & ; H_a^2 &= \frac{\sigma B_0^2 v}{\rho v_0^2} \text{ [Hartmann Number]} \\ Pr &= \frac{\mu C_p}{k_T} \text{ [Prandtl Number]} & ; Sc &= v/D \text{ [Schmidt Number]} \\ K &= \frac{v K_c}{v_0^2} \text{ [Chemical Reaction Parameter]} & ; J &= \frac{j v}{v_0^2} \text{ [Heat Absorption Parameter]} \end{aligned}$$

3. SOLUTION METHOD

The set of arranged dimensionless equations from (9) to (12), as a way to set boundary conditions (13) can be used to find the analytic solution using perturbation method. This approach can be completed by depicting perturbation parameter ($\epsilon \ll 1$) is very very small flow velocity u , temperature θ and concentration ϕ followed as.

$$U(x, y, t) = u_0(y) + \epsilon e^{(\lambda t)} u_1(y) + o(\epsilon^2) \quad \text{-----(14)}$$

$$P(x, y, t) = p_1(x) + \epsilon e^{(\lambda t)} p_1(y) + o(\epsilon^2) \quad \text{-----(15)}$$

$$T(x, y, t) = \theta_0(y) + \epsilon e^{(\lambda t)} \theta_1(y) + o(\epsilon^2) \quad \text{-----(16)}$$

$$C(x, y, t) = \phi_0(y) + \epsilon e^{(\lambda t)} \phi_1(y) + o(\epsilon^2) \quad \text{-----(17)}$$

We proceeding our problem omitting higher order terms i.e., $o(\epsilon^2)$, substituting above equation into basic equations (9) to (12) to obtain following pair of equations are u_0, θ_0, ϕ_0 and u_1, θ_1, ϕ_1

I. Zero Order Equations: (ϵ^0)

$$\left(\frac{d^2 u_0}{dy^2}\right) - \frac{du_0}{dy} - (\sigma^{*2} + H_a^2) u_0 = g_1 - Gr \theta_0 - Gc \phi_0 \quad \text{-----(18)}$$

$$\left(\frac{d^2 \theta_0}{dy^2}\right) - Pr \frac{d\theta_0}{dy} + J. Pr \theta_0 = 0 \quad \text{-----(19)}$$

$$\left(\frac{d^2 \phi_0}{dy^2}\right) - Sc \frac{d\phi_0}{dy} - K. Sc \phi_0 = 0 \quad \text{-----(20)}$$

In order to basic boundary conditions are,

$$\begin{aligned} \text{When } y = 0, \quad u_0 = 0, \theta_0 = \phi_0 = 1 & \quad \text{-----(21)} \\ \text{When } y = 1, \quad u_0 = 1, \theta_0 = \phi_0 = 0 & \end{aligned}$$

To obtain zeroth-order velocity (u_0), temperature (θ_0), concentration (ϕ_0), from (18) to (20) can be solved using boundary conditions (21). We get,

$$u_0 = A_9 e^{m_9 y} + A_{10} e^{m_{10} y} - \frac{g_1}{N} - \left(\frac{1}{(e^{m_1} - e^{m_2})}\right) (R_1 + R_2) - \left(\frac{1}{(e^{m_5} - e^{m_6})}\right) (C_1 + C_2) \quad \text{-----(22)}$$

$$\theta_0 = A_1 e^{m_1 y} + A_2 e^{m_2 y} \quad (\text{or}) \quad \frac{e^{m_1 y} (e^{m_1 - m_2} - 1) + e^{m_2 y}}{(e^{m_1} - e^{m_2})} \quad \text{-----(23)}$$

$$\phi_0 = A_5 e^{m_5 y} + A_6 e^{m_6 y} \quad (\text{or}) \quad \frac{e^{m_5 y} (e^{m_5 - m_6} - 1) + e^{m_6 y}}{(e^{m_5} - e^{m_6})} \quad \text{-----(24)}$$

II. First Order Equations: (ϵ^1)

$$\left(\frac{d^2 u_1}{dy^2}\right) - \frac{du_1}{dy} - (\sigma^{*2} + H_a^2 + \lambda) u_1 = n p_1 - Gr \theta_1 - Gc \phi_1 \quad \text{-----(25)}$$

$$\left(\frac{d^2 \theta_1}{dy^2}\right) - Pr \frac{d\theta_1}{dy} + (J Pr - \lambda Pr) \theta_1 = 0 \quad \text{-----(26)}$$

$$\left(\frac{d^2 \phi_1}{dy^2}\right) - Sc \frac{d\phi_1}{dy} - (K Sc + \lambda Sc) \phi_1 = 0 \quad \text{-----(27)}$$

In order to corresponding boundary conditions are,

$$\text{When } y = 0, \quad u_1 = 0, \theta_1 = \phi_1 = 1 \quad \text{-----(28)}$$

$$\text{When } y = 1, \quad u_1 = 1, \theta_1 = \phi_1 = 0$$

Simultaneously to obtain first order velocity (u_1), temperature (θ_1), Concentration (ϕ_1), from (25) to (27) can be solved using boundary conditions (28). We get,

$$u_1 = A_{11} e^{m_{11} y} + A_{12} e^{m_{12} y} - \left(\frac{1}{(e^{m_3} - e^{m_4})}\right) (R_3 + R_4) - \left(\frac{1}{(e^{m_7} - e^{m_8})}\right) (C_3 + C_4) \quad \text{-----(29)}$$

$$\theta_1 = A_3 e^{m_3 y} + A_4 e^{m_4 y} \quad (\text{or}) \quad \frac{e^{m_3 y} (e^{m_3 - m_4} - 1) + e^{m_4 y}}{(e^{m_3} - e^{m_4})} \quad \text{-----(30)}$$

$$\varphi_1 = A_7 e^{m_7 y} + A_8 e^{m_8 y} \quad (\text{or}) \quad \frac{e^{m_7 y}(e^{m_7 - e^{m_8} - 1}) + e^{m_8 y}}{(e^{m_7} - e^{m_8})} \quad \text{-----(31)}$$

Employ complete solution of base and perturb parts are (22) to (24) and (29) to (31) in (14) to (17), we get final form of the solution is the summation of base partfactor and perturb element offers the corresponding Velocity, Temperature, Concentration of fluid molecule as given below:

$$\begin{aligned} U(y, t) &= (u_0 + \epsilon e^{(\lambda t)} u_1) \\ T(y, t) &= (\theta_0 + \epsilon e^{(\lambda t)} \theta_1) \\ C(y, t) &= (\varphi_0 + \epsilon e^{(\lambda t)} \varphi_1) \end{aligned}$$

4. RESULTS AND DISCUSSION

The current observation is used to assess numerical computation of the analytic result for the subsequent fluid particles namely velocity, temperature, concentration distributions for numerous amounts of physical specification can express the characteristic of the fluid flow. Heat and Mass Transfer computed analytically also, their outcomes have been portrayed graphically with the assist of MATLAB. Throughout the computation we employ corresponding values to classify the graph ($t = 0.01, \mu = 3 \times 10^{-6}; \rho = 992.2 \times 10^{-15}, g = 9.81 \times 10^6, \lambda = 0.3, \epsilon = 0.01, Gr = 0.5, Gc = 0.5, Pr = 0.7, Sc = 0.60, \sigma^* = 0.2, K = 0.3, J = 0.0224, H_a = 0.3$) Sudaporn Poopraet al. [10], excepting that the supplementary values of parameter kept as fixed state. We compute the various values of Grashof Number, Solutal Grashof Number, Chemical Reaction Parameter, Hartmann Number, Porosity Parameter, Prandtl Number, Schmidt Number.

Effect of various parameters of Velocity distribution (U) with respect to y:

(i) Fig.2. Shows that various Effect of Magnetic range in the velocity distribution:

This force is known as Lorentz force. From the below graph, we understand that pleural fluid flow of the Velocity decreases with increasing HARTMANN Number.

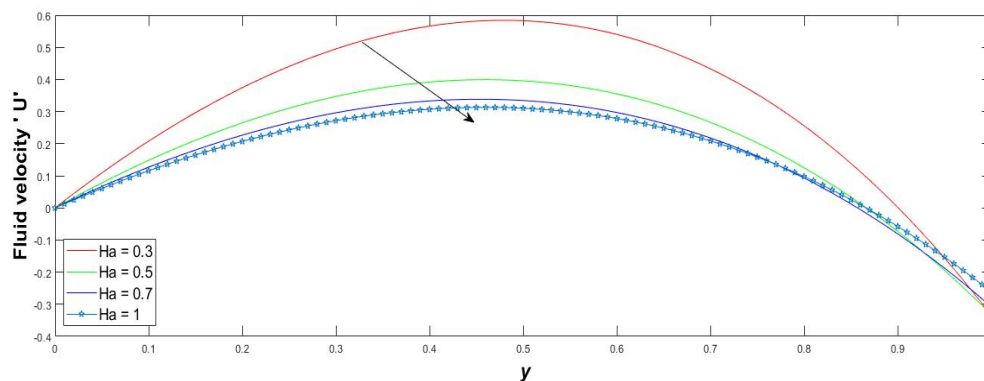


Fig.2 Velocity Field for different H_a .

(ii) Fig.3 shows that Effect of porosity parameter in the velocity distribution:

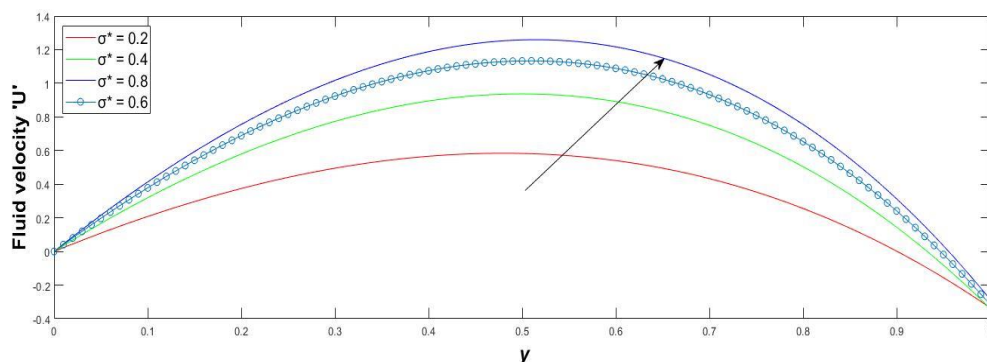


Fig.3 Velocity Field for different σ^* .

Porosity describes a measure of the "Empty Space" in a solid material, its volume lies between 0 to 1. we perceived that velocity of the fluid increases with increasing Porosity permeable parameter
(iii) Fig.4 shows that Effect of Grashof number in the velocity distribution:

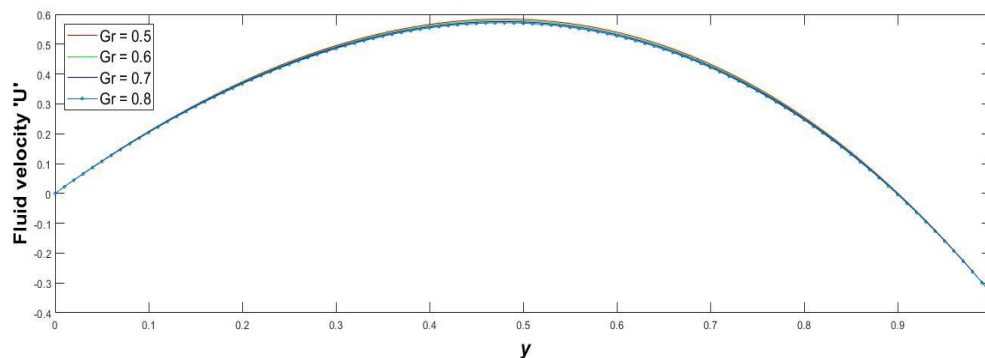


Fig.4 Velocity Field for different Gr.

(iv) Fig. 5 shows that Effect of SolutalGrashof number in the velocity distribution:

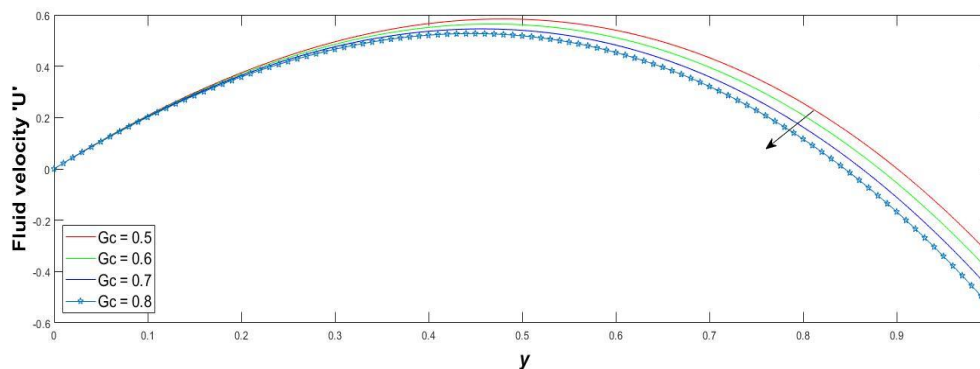


Fig.5 Velocity Field for different Gc.

Above graphs are representing in the form of pictorially velocity of the pleural fluid decreases gradually while increasing Grashof and SolutalGrashof parameter values. It is clear that inside the lung, there is a buoyancy flow occurs during the fluid flow due to acceleration of gravitational force. It represents the domination of buoyancy force for the convection comparing to the viscous force. Buoyant force caused by a temperature gradient and concentration gradient. When the fluid is at rest two gradients would be absent. The variations of the Velocity are higher by the act of toxin (COVID -19) than fluid segment, while the solute attention of the solid particle adjustments. That is because of theexistence ofCOVID-19 contamination interiorof the respiratory tract.It's miles clear thattremendous changes in the fluid Velocity havea major influence impact of contaminant particles when compared with pure fluid profile.

In addition, following remarks are made when temperature distributions are computed.

Effect of various parameters of Temperature distribution (T) with respect to y:

(v) Fig. 6 Shows that Effect of Prandtl Number in the Temperature distribution:

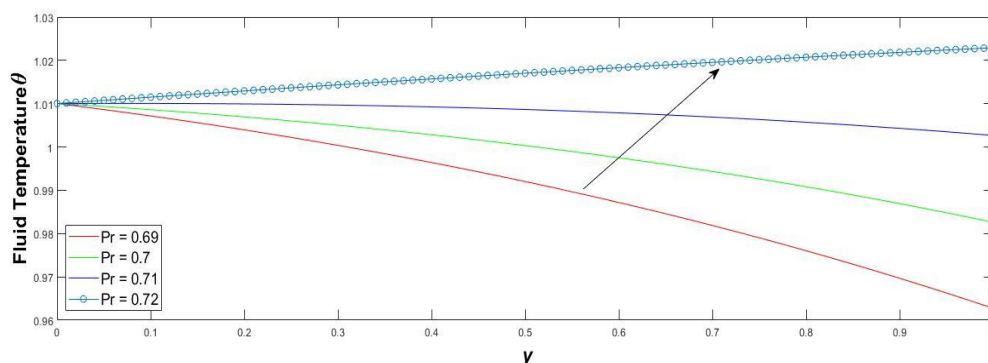


Fig.6 Temperature Field for different Pr.

The Prandtl Number restricts the relative density of the motion and thermal boundary layers. Also, it signifies the relative speed with which momentum and energy propagates through fluid. From this we observed that enhances Prandtl Number results increases in thermal boundary layers simultaneously Temperature increased inside the boundary layer.

(vi) Fig.7 Shows that Effect of Heat Absorption Parameter in the Temperature distribution:

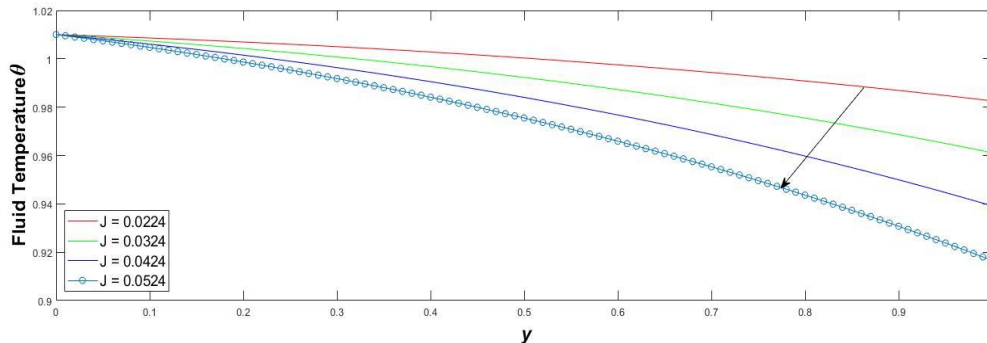


Fig.7 Temperature Field for different J.

Above graph displays temperature profile decreases with increasing Heat absorption parameter.

Effect of various parameters of Concentration distribution (C) with respect to y:

(vii) Fig.8 shows that Effect of numerous Schmidt Number in the Concentration distribution

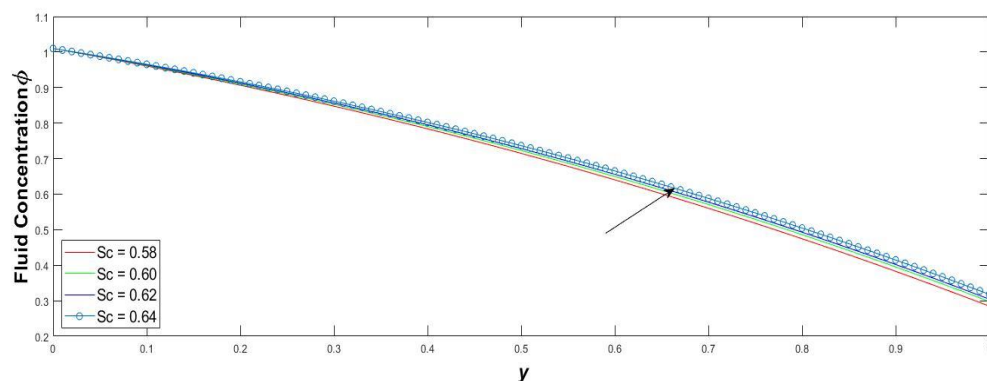


Fig.8 Concentration Field for different Sc.

(viii) Fig.9 Shows that Effect of numerous Chemical Reaction parameter in the concentration distribution:

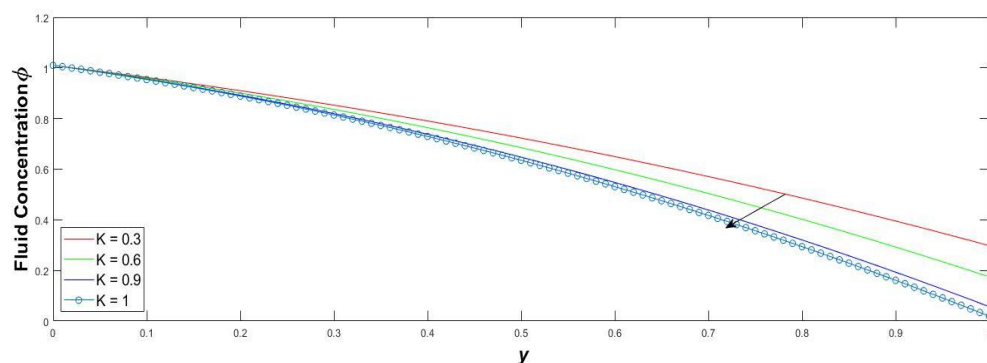


Fig.9 Concentration Field for different K.

Subsequently Concentration profile decreases of increasing Schmidt number and increases of Chemical reaction parameter. It shows that massive differences in COVID-19 diffusion rate by the reaction of chemical. The heat transfer rates increase and mass transfer decrease ultimately according to the nature of the fluid flow with increased buoyancy ratio.

5. CONCLUSION

The dimensionless above governing equations are solved analytically with the help of perturbation technique. We have concluded that heat and mass transfer on an unsteady magnetic field with natural convective flow of human respiratory tract due to buoyancy effect of lungs and chemical reaction inside the pleural cavity.

From the above results we summarized the major findings are given below:

- The velocity of a fluid flow decreases monotonically for increasing Hartmann number.
- Velocity of fluid flow decreases gradually both increased Grashof and Solutal Grashof number.
- The velocity distribution increasing with moderate increased Porosity parameter.
- Temperature of fluid flow increases due to increase in the thermal diffusion Prandtl number.
- Concentration profile increased due to increased Schmidt number.
- There is a significant fall due to increased Chemical reaction parameter and considerably reduces at prominent point.

6. APPENDIX

$$\begin{aligned}
 Q &= H_a^2 + \sigma^{*2} & ; & \quad s = J \cdot Pr & ; & \quad B = H_a^2 + \sigma^{*2} + \lambda \\
 g_1 &= \frac{\partial p_0}{\partial x} & ; & \quad \omega = K \cdot Sc \\
 m_1 &= \frac{(Pr) + \sqrt{(Pr)^2 - 4 J Pr}}{2} & ; & \quad m_2 = \frac{(Pr) - \sqrt{(Pr)^2 - 4 J Pr}}{2} \\
 m_3 &= \frac{(Pr) + \sqrt{(Pr)^2 - 4 Pr(J-\lambda)}}{2} & ; & \quad m_4 = \frac{(Pr) - \sqrt{(Pr)^2 - 4 Pr(J-\lambda)}}{2} \\
 m_5 &= \frac{(Sc) + \sqrt{(Sc)^2 - 4 K Sc}}{2} & ; & \quad m_6 = \frac{(Sc) - \sqrt{(Sc)^2 - 4 K Sc}}{2} \\
 m_7 &= \frac{(Sc) + \sqrt{(Sc)^2 + 4 Sc(K+\lambda)}}{2} & ; & \quad m_8 = \frac{(Sc) - \sqrt{(Sc)^2 + 4 Sc(K+\lambda)}}{2} \\
 m_9 &= \frac{1 + \sqrt{1 + 4(H_a^2 + \sigma^{*2})}}{2} & ; & \quad m_{10} = \frac{1 - \sqrt{1 + 4(H_a^2 + \sigma^{*2})}}{2} \\
 m_{11} &= \frac{1 + \sqrt{1 + 4(H_a^2 + \sigma^{*2} + \lambda)}}{2} & ; & \quad m_{12} = \frac{1 - \sqrt{1 + 4(H_a^2 + \sigma^{*2} + \lambda)}}{2} \\
 A_1 &= 1 - A_2 & ; & \quad A_2 = \frac{1}{(e^{m_1} - e^{m_2})} \\
 A_3 &= 1 - A_4 & ; & \quad A_4 = \frac{1}{(e^{m_3} - e^{m_4})} \\
 A_5 &= 1 - A_6 & ; & \quad A_6 = \frac{1}{(e^{m_5} - e^{m_6})} \\
 A_7 &= 1 - A_8 & ; & \quad A_8 = \frac{1}{(e^{m_7} - e^{m_8})} \\
 A_9 &= -A_{10} + \frac{g}{Q} + \left(\frac{1}{(e^{m_1} - e^{m_2})} \right) (R_1 + R_2) + \left(\frac{1}{(e^{m_5} - e^{m_6})} \right) (C_1 + C_2) & ; \\
 A_{10} &= \left(\frac{e^{m_9} - 1}{e^{m_9} - e^{m_{10}}} \right) \left(\frac{g}{Q} + \left(\frac{1}{(e^{m_1} - e^{m_2})} \right) (R_1 + R_2) + \left(\frac{1}{(e^{m_5} - e^{m_6})} \right) (C_1 + C_2) \right) & ; \\
 A_{11} &= -A_{12} + \left(\frac{1}{(e^{m_3} - e^{m_4})} \right) (R_3 + R_4) + \left(\frac{1}{(e^{m_7} - e^{m_8})} \right) (C_3 + C_4) & ; \\
 A_{12} &= \left(\frac{e^{m_{11}} - 1}{e^{m_{11}} - e^{m_{12}}} \right) \left(\left(\frac{1}{(e^{m_3} - e^{m_4})} \right) (R_3 + R_4) + \left(\frac{1}{(e^{m_7} - e^{m_8})} \right) (C_3 + C_4) \right) & ; \\
 R_1 &= \frac{Gr(e^{m_1} - e^{m_2} - 1)}{m_1^2 - m_1 - Q} & ; & \quad R_2 = \frac{Gr e^{m_2 y}}{m_2^2 - m_2 - Q} \\
 R_3 &= \frac{Gr(e^{m_3} - e^{m_4} - 1)}{m_3^2 - m_3 - B} & ; & \quad R_4 = \frac{Gr e^{m_4 y}}{m_4^2 - m_4 - B} \\
 C_1 &= \frac{Gc(e^{m_5} - e^{m_6} - 1)}{m_5^2 - m_5 - Q} & ; & \quad C_2 = \frac{Gc e^{m_6 y}}{m_6^2 - m_6 - Q} \\
 C_3 &= \frac{Gc(e^{m_7} - e^{m_8} - 1)}{m_7^2 - m_7 - B} & ; & \quad C_4 = \frac{Gc e^{m_8 y}}{m_8^2 - m_8 - B}
 \end{aligned}$$

7. NOMENCLATURE

x – cartesian co – ordinate onward the portion

- y – cartesian coordinate perpendicular to the portion
 u – dimensional velocity component u onward x directions
 v – dimensional velocity component u onward y directions
 g – gravitational acceleration
 p – pressure of the fluid
 ρ – fluid density
 μ – dynamic viscosity of the pleural fluid
 ν – kinematic viscosity of the pleural fluid
 k_1 – dimensional permeability of the porous medium
 σ – magnetic permeability of the fluid
 B_0 – Coefficient of magnetic field
 β – Coefficient of volumetric thermal expansion
 $\beta^* - Co$ – efficient of volumetric concentration expansion
 T – dimensional fluid temperature
 T_w – temperature of the surface wall
 T_0 – Initial temperature
 C_p – Specific heat at Constant pressure
 K_T – thermal conductivity
 J – Coefficient of spatial heat absorption
 C – Dimensional fluid Concentration
 C_w – Concentration of the surface wall
 C_0 – Initial concentration
 D – Mass diffusivity
 K – Chemical Reaction Parameter
 Gr – Grashof Number
 Gc – Solutal Grashof Number
 Ha – Hartmann Number
 Pr – Prandtl Number
 Sc – Schmidt Number
 σ^* – Porosity Parameter

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