

Fuzzy Mean e -Open and e -Closed Sets

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Abstract

The notions of fuzzy mean e -open and e -closed sets is established. Moreover, some comparative study of these with other fuzzy mappings are investigated. Finally, we extend fuzzy mean e -open to fuzzy para e -open sets in fuzzy topology.

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1. Introduction

Fuzzy sets were established by Zadeh [10] and the perception of fuzzy topology instigated by Chang [2] in 1968. The ideas of fuzzy minimal (resp. maximal open) [3] sets explored in [3]. Subsequently the concepts of fuzzy mean open set investigated by Swaminathan [9]. On combining fuzzy mean open [9] and fuzzy paraopen open [4] sets, we extend the perception of fuzzy mean open (resp. closed) sets and from which we investigate some results.

The following terminologies “fuzzy e -open (resp.closed), fuzzy e -mean open(resp.closed), fuzzy minimal e -open(resp.maximal), fuzzyminimal e -closed set, (resp.maximal), fuzzy e -paraopen(resp.para-closed) and fuzzy e -connected topological space respectively abbreviated as F_e -O, F_e -C, FME_e -O, FME_e -C, FMI_e -O, FMA_e -O, FMI_e -C, FMA_e -C, F_e -PO, F_e -PC and F_e -CTS. Entire paper F stands for fuzzy topology (F, τ) ”.

2. Preliminaries

Definition 2.1. A fuzzy subset $\beta \in \mathbb{F}$ is said to be fuzzy regular open [1] if $\beta = \text{Int} [Cl(\beta)]$

The union of all fuzzy regular open sets contained in fuzzy subset $\beta \in \mathbb{F}$ is F_e -interior of β . If $\beta = \text{Int}\delta(\beta)$ then fuzzy subset β is called F_e -O [8] such that its complement is called F_e -C (i.e, $\beta = Cl\delta(\beta)$).

Definition 2.2. [5] A proper nonzero F_e -O set $\beta \in \mathbb{F}$ is called (i) FMI_e -O if only F_e -O sets contained in β . are β and 0 (ii) FMA_e -O if only F_e -O sets containing β are 1 and β .

Definition 2.3. A FO set $\mu \in \mathbb{F}$ is said to be a FPO [4]set if it is neither FMIO nor FMAO set.

3. Fuzzy e -Paraopen and e -Paraclosed Sets

Definition 3.1. A F_e -O set $\zeta \subset \mathbb{F}$ which is neither FMI_e -O nor FMA_e -O set is said to be F_e -PO set.

Definition 3.2. A F_e -C set $\alpha \subset \mathbb{F}$ is said to be a F_e -PC set iff its complement $1 - \alpha$ is F_e -PO set.

Remark 3.1. The converse of the statement: Every F_e -PO set (resp. F_e -PC) is a FO set(resp.FC set). Need not to be true proven by following example.

Example 3.2.

Remark 3.3. Union (resp.intersection) of F_e -PO (resp. F_e -PC) sets need not be F_e -PO

(resp. F_e -PC) set.

Theorem 3.4. Let \mathbb{F} be a FTS and α be a nonempty proper F_e -PO subset of \mathbb{F} , then \exists a FMI_e -O set ζ with $\zeta < \alpha$.

Proof. Clearly $\zeta < \alpha$ as per the FMI_e -O set definition.

Theorem 3.5. Let α be a nonempty proper F_e -PO subset of a FTS \mathbb{F} , then \exists a ψ FMA_e -O set with $\alpha < \psi$.

Proof. Clearly $\alpha < \psi$ as per the FMA_e -O set definition.

Theorem 3.6. Suppose that \mathbb{F} is a FTS, then

- (i) $\zeta \wedge \lambda = 0$ or $\zeta < \lambda$ for any F e -PO ζ and a FMI e -O set λ . (ii) $\zeta \vee \lambda = 1$ or $\zeta < \lambda$ for any F e -PO ζ and a FMA e -O set λ . (iii) Intersection of F e -PO sets is either F e -PO or FMI e -O set.

Proof. (i) For any F e -PO set ζ and a FMI e -O open set λ in \mathbb{F} . Then $\zeta \wedge \lambda = 0$ or $\zeta \wedge \lambda \neq 0$. If $\zeta \wedge \lambda = 0$, then proof could be over. Assume $\zeta \wedge \lambda \neq 0$. Then we write $\zeta \wedge \lambda$ is a FO set and $\zeta \wedge \lambda < \zeta$. Hence $\zeta < \lambda$.

(ii) For any F e -PO set ζ and a FMA e -O set λ in \mathbb{F} . Then $\zeta \vee \lambda = 1$ or $\zeta \vee \lambda \neq 1$. If $\zeta \vee \lambda = 1$, then proof could be over. Assume $\zeta \vee \lambda \neq 1$. Clearly, $\zeta \vee \lambda$ is a FO set and $\lambda < \zeta \vee \lambda$. Hence λ is a FMA e -O set, $\zeta \vee \lambda = \lambda$ implies $\zeta < \lambda$.

(iii) Let ζ and λ be a F e -PO sets in \mathbb{F} . If $\zeta \wedge \lambda$ is a F e -PO set, then proof could be over. Suppose $\zeta \wedge \lambda$ is not a F e -PO set. By definition, $\zeta \wedge \lambda$ is a FMI e -O or FMA e -O set. If $\zeta \wedge \lambda$ is a FMI e -O set, then proof could be over. Suppose $\zeta \wedge \lambda$ is a FMA e -O set. Now $\zeta \wedge \lambda < \zeta$ and $\zeta \wedge \lambda < \lambda$ contradicting the fact that ζ and λ are F e -PO sets. Hence, $\zeta \wedge \lambda$ is not a FMA e -O set. (i.e.) $\zeta \wedge \lambda$ is a FMI e -O set.

Theorem 3.7. A subset λ of a FTS \mathbb{F} is F e -PC iff it is neither FMA e -C nor FMI e -C set.

Proof. The complement of FMI e -O set and FMA e -O set are FMA e -C set and FMI e -C set respectively.

Theorem 3.8. Let λ be a nonempty F e -PC subset of a FTS \mathbb{F} . Then \exists a FMI e -C set ψ with $\psi < \lambda$.

Proof. Clearly by FMI e -C set definition, it follows that $\psi < \lambda$.

Theorem 3.9. Suppose that λ is a nonempty F e -PC subset of FTS \mathbb{F} then \exists a FMA e -C set κ such that $\lambda < \kappa$.

Proof. Clearly by FMA e -C set definition, it follows that $\lambda < \kappa$.

Theorem 3.10. Suppose that \mathbb{F} is a FTS then

- (i) $\kappa \wedge \eta = 0$ or $\eta < \kappa$ for any F e -PC set κ and FMI e -C set η . (ii) $\kappa \vee \zeta = 1$ or $\kappa < \zeta$ for any F e -PC set κ and FMA e -C set ζ .
- (iii) Intersection of F e -PC sets is either F e -PC or FMI e -C set.

Proof. (i) Suppose that κ is a F e -PC and η is a FMI e -C set in \mathbb{F} . Then $(1 - \kappa)$ is F e -PO and $(1 - \eta)$ is FMA e -O set in \mathbb{F} . Then by Theorem 3.6 (ii) $(1 - \kappa) \vee (1 - \eta) = \mathbb{F}$ or $(1 - \kappa) < (1 - \eta)$ implying $1 - (\kappa \wedge \eta) = 1$ or $\eta < \kappa$. Hence, $\kappa \wedge \eta = 0$ or $\eta < \kappa$.

(ii) Suppose that κ is a F e -PC and ζ is a FMA e -C set in \mathbb{F} . Then $(1 - \kappa)$ is F e -PO and $(1 - \zeta)$ is FMI e -O sets in \mathbb{F} . Then by Theorem 3.6(i) $(1 - \kappa) \wedge (1 - \zeta) = 0$ or $1 - \zeta < 1 - \kappa$ implying $1 - (\kappa \vee \zeta) = 0$ or $\kappa < \zeta$. Hence, $\kappa \vee \zeta = 1$ or $\kappa < \zeta$.

(iii) Suppose that κ and ξ is a F e -PC sets in \mathbb{F} . If $\kappa \wedge \xi$ is a F e -PC set, then proof could be over. Suppose $\kappa \wedge \xi$ is not a F e -PC set. Then clearly, $\kappa \wedge \xi$ is FMI e -C or FMA e -C set. Suppose $\kappa \wedge \xi$ is a FMI e -C set, then proof could be over. Suppose $\kappa \wedge \xi$ is a FMA e -C set. Now $\kappa < \kappa \wedge \xi$ and $\xi < \kappa \wedge \xi$ a contradiction for κ and ξ are F e -PC sets. Hence, $\kappa \wedge \xi$ is not a FMA e -C set. (i.e.) $\kappa \wedge \xi$ is a FMI e -C set.

4. Fuzzy Mean e -Open and e -Closed Sets

Definition 4.1. A F e -O set $\psi \subset \mathbb{F}$ is said to be a FME e -O set if $\exists \omega_1, \omega_2 (\omega_1 \neq \psi)$ two distinct proper F e -O sets such that $\omega_1 < \psi < \omega_2$.

Remark 4.1. It could be understood from the succeeding example that the union and intersection of FME e -O need not be FME e -O sets.

Example 4.2. Let $\mathbb{F} = \{x, y, z, w\}$. Then fuzzy sets

$$\begin{aligned} \omega_1 &= \{(0.5, x), (0.4, y), (0.4, z), (0.5, w)\} ; \\ \omega_2 &= \{(0.5, x), (0.4, y), (0.6, z), (0.5, w)\} ; \\ \omega_3 &= \{(0.5, x), (0.6, y), (0.4, z), (0.5, w)\} \end{aligned}$$

and $\omega_4 = \{(0.5, x), (0.6, y), (0.6, z), (0.5, w)\}$ of the fuzzy topology $\tau = \{0, \omega_1, \omega_2, \omega_3, \omega_4, 1\}$. Hence ω_2 and ω_3 are FME e -O sets but their union $\omega_2 \vee \omega_3 = \omega_4$ and intersection $\omega_2 \wedge \omega_3 = \omega_1$ are not FME e -O sets.

Definition 4.2. A F e -C set $v \subset \mathbb{F}$ is said to be a FME e -C set if two F e -C sets $\xi_1 \neq \xi_2 (\neq v)$ such that $\xi_1 < v < \xi_2$.

Definition 4.3. A F e -O set $\zeta \subset \mathbb{F}$ which is neither FMI e -O nor FMA e -O set is said to be F e -PO set where its complement is known to be F e -PC set.

Theorem 4.3. A F e -O set of a fts is a FME e -O set iff its complement is a FME e -C set.

Proof. By deploying definition 4.1 for any FME e -O set ψ in \mathbb{F} we have $\omega_1 < \psi < \omega_2$

implying that $1 - \omega_2 < 1 - \psi < 1 - \omega_1$. Clearly $1 - \omega_2 \neq 0, 1 - \psi$ and $1 - \omega_1 \neq 1 - \psi, 1$. Hence $1 - \psi$ is a FME e -C set.

Conversely, Let $1 - \psi$ is a FME e -C set for any FME e -O set ψ in \mathbb{F} . By definition 4.2, F e -C sets $\xi_1 \neq 0, 1 - \psi$ and $\xi_2 \neq 1, 1 - \psi$ such that $\xi_1 < 1 - \psi < \xi_2$ implying that $1 - \xi_2 < \psi < 1 - \xi_1$. As $\xi_2 \neq 0, \psi$ and $1 - \xi_1 \neq \psi, 1$; ψ is a FME e -O set.

Theorem 4.4. A proper F e -PO set is a FME e -O set and vice-e-versa.

Proof. The proof of necessary part is obvious by theorem 1.7 [9].

Conversely, let ψ be a proper FME e -O set in \mathbb{F} . Then two F e -O sets $\zeta_1 \neq \zeta_2$ such that $\zeta_1 < \psi < \zeta_2$. Clearly ψ is neither FMI e -O nor FMA e -O set as $\zeta_1 \neq 0, \psi$ and $\zeta_2 \neq \psi, 1$. As $\psi \neq 0, 1$, ψ is a proper F e -PO set.

Theorem 4.5. A proper F e -PC set is a FME e -C set and vice-e-versa.

Proof. The proof of necessary part is obvious by theorem 1.10 [9].

Conversely, let ϑ be a proper FME e -C set in \mathbb{F} . Then two F e -C sets $v_1 \neq v_2 \neq \vartheta$ such that $v_1 < \vartheta < v_2$. Clearly ϑ is neither a FMI e -C nor a FMA e -C set as $v_1 \neq 0, \vartheta$ and $v_2 \neq 1, \vartheta$. As $\vartheta \neq 0, 1$, ϑ is a proper F e -PC set.

Theorem 4.6. ([5]) Let \mathbb{F} be a fts.

(i) If ζ is a FMI e -O and ξ is a F e -O sets in \mathbb{F} , then $\zeta \wedge \xi = 0$ or $\zeta < \xi$. (ii) If ζ and κ are FMI e -O sets, then $\zeta \wedge \kappa = 0$ or $\zeta = \kappa$.

Theorem 4.7. ([5]) Let \mathbb{F} be a fts.

(i) If ζ is a FMA e -O and ξ is a F e -O sets in \mathbb{F} , then $\zeta \vee \xi = 1$ or $\xi < \zeta$. (ii) If ζ and κ are FMA e -O set, then $\zeta \vee \kappa = 1$ or $\zeta = \kappa$.

Theorem 4.8. If ξ_1 is a FMA e -O set and ξ_2 is a FMI e -O set of a fts \mathbb{F} , then either $\xi_2 < \xi_1$ or \mathbb{F} is fuzzy e -disconnected.

Theorem 4.9. Let a F e -CTS \mathbb{F} contain a FMA e -O set ζ_2 , a FMI e -O set $\zeta_1 \neq \zeta_2$ and a proper F e -O set $\xi \neq \zeta_1, \zeta_2$. Then exactly one of the succeeding could be true on \mathbb{F} :

(i) ξ is a FME e -O set with $\zeta_1 < \xi < \zeta_2$.

(ii) $\zeta_1 < 1 - \xi < \zeta_2$.

(iii) $\zeta_1 < \xi, \zeta_1 \vee \xi = 1$ and $\zeta_2 \wedge \xi \neq 0$.

(iv) $\xi < \zeta_2, \zeta_1 \wedge \zeta_2 = 0$ and $\zeta_1 \vee \zeta_2 \neq 1$.

Proof. By deploying theorem 4.8, a FMI e -O set $\zeta_1 < \zeta_2$ a FMA e -O set. This implies either $\zeta_1 < \xi$ or $\zeta_1 \wedge \xi = 0$ and $\xi < \zeta_2$ or $\zeta_2 \vee \xi = 1$. Hence the feasible combinations are (i) $\zeta_1 < \xi < \zeta_2$, (ii) $\zeta_1 \wedge \xi = 0; \zeta_2 \vee \xi = 1$, (iii) $\zeta_1 < \xi; \zeta_2 \vee \xi = 1$, (iv) $\zeta_1 \wedge \xi = 0$ and $\xi < \zeta_2$.

Clearly $\zeta_1 < 1 - \xi < \zeta_2$ if (ii) is true. Also, $0 \neq \zeta_1 < \zeta_1 \wedge \xi$ as $\zeta_1 < \zeta_2$ and (iii) is true. Again $\zeta_1 \vee \xi < \zeta_2 \neq 1$ as $\zeta_1 < \zeta_2$ and (iv) is true.

Case(I): As (i) and (ii) are true, then $\zeta_1 < \xi \vee (1 - \xi) < \zeta_2$ and $\zeta_1 < \xi \wedge (1 - \xi) < \zeta_2$. As $\zeta_1 < \xi \vee (1 - \xi) < \zeta_2$ $\zeta_1 < 1 < \zeta_2$ then $\zeta_2 = 1$, an absurd result.

Similarly, for $\zeta_1 < \xi \wedge (1 - \xi) < \zeta_2$ we get $\zeta_1 = 0$, an absurd result.

Case(II): As both (i),(iii) are true, then $\xi < \zeta_2$ and $\zeta_2 \vee \xi = 1$ gives $\zeta_2 = 1$, an absurd result.

Case(III): As both (i),(iv) are true, then $\zeta_1 < \xi$ and $\zeta_1 \wedge \xi = 0$ gives $\zeta_1 = 0$, an absurd result.

Case(IV): As both (ii),(iii) are true, then $\zeta_1 < 1 - \xi$ and $\zeta_1 < \xi$ gives $\zeta_1 = 0$, an absurd result.

Case(V): As both (ii),(iv) are true, then $1 - \xi < \zeta_2$ and $\xi < \zeta_2$ gives $\zeta_2 = 1$, an absurd result.

Case(VI): As both (iii),(iv) are true, then $\zeta_1 < \xi < \zeta_2$, $\zeta_2 \vee \xi = 1$ and $\zeta_1 \wedge \xi = 0$. Clearly $\zeta_2 = 1$ as $\xi < \zeta_2$ and $\zeta_2 \vee \xi = 1$ a contradiction. Similarly, we get $\zeta_1 = 0$ as $\zeta_1 < \xi$ and $\zeta_1 \wedge \xi = 0$ a contradiction.

Theorem 4.10. Let a F e -CTS \mathbb{F} contain a FMA e -C set v_2 , a FMI e -C set v_1 with $v_1 \neq v_2$ and a proper F e -C set $\beta \neq v_1, v_2$. Then any one of them could be true on \mathbb{F} :

- (i) β is a FME e -C set such that $v_1 < \beta < v_2$.
- (ii) $v_1 < 1 - \beta < v_2$.
- (iii) $\beta < v_2$, $v_1 \wedge \beta = 0$ and $v_1 \vee \beta \neq 1$
- (iv) $v_1 < \beta$, $v_2 \vee \beta = 1$ and $v_2 \wedge \beta \neq 0$.

Proof. Let \mathbb{F} be a F e -CTS containing $1 - v_1$, a FMA e -O set; $1 - v_2$ a FMI e -O set and $1 - \beta$ a proper F e -O set such that $1 - v_1 \neq 1 - v_2$ and $1 - \beta \neq 1 - v_1, 1 - v_2$. By deploying Theorem 4.9, any one of them could be true:

- (i) For any FME e -O set $1 - \beta$ we get $v_1 < \beta < v_2$ as $1 - v_2 < 1 - \beta < 1 - v_1$, Hence, β is a FME e -C set.
- (ii) Clearly, $v_1 < 1 - \beta < v_2$. as $1 - v_2 < 1 - (1 - \beta) < 1 - v_1$
- (iii) If $1 - v_2 < 1 - \beta$; $(1 - v_1) \vee (1 - \beta) = 1$ and $(1 - v_1) \wedge (1 - \beta) \neq 0$ then $\beta < v_2$; $v_1 \wedge \beta = 0$ and $v_1 \vee \beta \neq 1$.
- (iv) If $1 - \beta < 1 - v_1$; $(1 - v_2) \wedge (1 - \beta) = 0$ and $(1 - v_2) \vee (1 - \beta) \neq 1$ then $v_1 < \beta$; $v_2 \vee \beta = 1$ and $v_2 \wedge \beta \neq 0$.

Theorem 4.11. Let two distinct FMA e -O and FME e -O sets in \mathbb{F} . Then intersection of

the two FMA e -O sets is nonzero.

Proof. By deploying theorem 4.7, $\kappa_1 \vee \kappa_2 = 1$ for any two distinct FMA e -O sets κ_1 and κ_2 in \mathbb{F} . Let σ be a FME e -O set in a fts \mathbb{F} then σ is neither FMA e -O nor FMI e -O such that, $\sigma \neq \kappa_1, \kappa_2$ and $\sigma \neq 1$. By Theorem 4.7, we get $\sigma \not\subseteq \kappa_1$ or $\sigma \vee \kappa_1 = 1$ and $\sigma \not\subseteq \kappa_2$ or $\sigma \vee \kappa_2 = 1$. The feasible combinations are (i) $\sigma \not\subseteq \kappa_1$ and $\sigma \not\subseteq \kappa_2$, (ii) $\sigma \not\subseteq \kappa_1$ and $\sigma \vee \kappa_2 = 1$, (iii) $\sigma \not\subseteq \kappa_2$ and $\sigma \vee \kappa_1 = 1$ and (iv) $\sigma \vee \kappa_1 = 1$ and $\sigma \vee \kappa_2 = 1$. Case (I): Obviously true.

Case (II): By assuming $\sigma \wedge \kappa_2 \neq 0$, we have to prove that $\kappa_1 \wedge \kappa_2 \neq 0$. As $\sigma \wedge \kappa_2 \neq 0$ and $\sigma \not\subseteq \kappa_1$, then there exists $x\alpha \in \kappa_1$ such that $x\alpha \neq \kappa_2$. Since $\sigma \vee \kappa_2 = 1$, $x\alpha \in \kappa_2$. So, $\kappa_1 \wedge \kappa_2 \neq 0$.

Case (III): Similar to previous case.

Case (IV): As $\sigma \vee \kappa_1 = 1$; $\sigma \vee \kappa_2 = 1$ imply that $\sigma \vee (\kappa_1 \wedge \kappa_2) = 1$ then $\sigma = 1$ if $\kappa_1 \wedge \kappa_2 = 0$. Again $\kappa_1 \wedge \kappa_2 \neq 0$ as $\sigma \neq 1$.

Theorem 4.12. Let two distinct FMI e -O and FME e -O sets in \mathbb{F} . Then union of the two

FMI e -O sets is not equal to 1.

Proof. By deploying theorem 4.6, we have $\kappa_1 \vee \kappa_2 = 0$ for any two distinct FMI e -O sets κ_1, κ_2 in a fts \mathbb{F} . Let σ being a FME e -O set in \mathbb{F} , then it is neither FMA e -O nor FMI e -O. Hence, $\sigma \neq \kappa_1, \kappa_2$ and $\sigma \neq 0, 1$. By theorem 4.6, we get $\kappa_1 \not\subseteq \sigma$ or $\sigma \wedge \kappa_1 = 0$ and $\kappa_2 \not\subseteq \sigma$ or $\sigma \wedge \kappa_2 = 0$. The possible combinations are (I) $\kappa_1 \not\subseteq \sigma$ and $\kappa_2 \not\subseteq \sigma$, (II) $\kappa_1 \not\subseteq \sigma$ and $\sigma \wedge \kappa_2 = 0$, (III) $\kappa_2 \not\subseteq \sigma$ and $\sigma \wedge \kappa_1 = 0$ and (IV) $\sigma \wedge \kappa_1 = 0$ and $\sigma \wedge \kappa_2 = 0$ as $\sigma \neq 1$.

Case I: Obviously, if $\kappa_1 \not\subseteq \sigma$ and $\kappa_2 \not\subseteq \sigma$ then $\kappa_1 \vee \kappa_2 \neq 1$.

Case II: Suppose that $\sigma \vee \kappa_2 \neq 1$. Since $\kappa_1 \not\subseteq \sigma$, then there exists $x\alpha \in \sigma$ such that $x\alpha \neq \kappa_1$.

As $\sigma \wedge \kappa_2 = 0$; clearly $x\alpha \neq \kappa_2$. Hence, $x\alpha \neq \kappa_1, \kappa_2$ imply that $\kappa_1 \vee \kappa_2 \neq 1$.

Case III: Similar to previous case.

Case IV: As $\sigma \wedge \kappa_1 = 0$; $\sigma \wedge \kappa_2 = 0$ imply that $\sigma \wedge (\kappa_1 \vee \kappa_2) = 0$ then $\sigma = 0$ if $\kappa_1 \vee \kappa_2 = 1$.

Clearly $\kappa_1 \vee \kappa_2 \neq 1$ as $\sigma \neq 0$.

“On combining theorems 4.11 and 4.12, we get theorems 4.13 and 4.14 and the proofs succeeded by theorems 4.11 and 4.12.”

Theorem 4.13. Let κ and ϱ be distinct FMA e -C and FME e -C sets in a FTS respectively. Then the intersection of two FMA e -O sets is nonzero.

Theorem 4.14. Let ζ and ξ be distinct FMI e -C and FME e -C sets in a FTS respectively. Then the union of two FMI e -C sets is not equal to 1.

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