

# Design and Stress Analysis of Face Gear Drive in Automobile

**Sudhakar, S.Venkatesan, K.Hariharan**, Assistant Professor, Department of Mechanical Engineering, Dhanalakshmi Srinivasan College of Engineering and Technology, Mamallapuram

## ABSTRACT:

In automobiles, Gear drive failures are the major consequence which causes break downs; this can be optimized by new developments in design, and stress analysis of gear drives. The main contents of the paper are: (i) identification of transmission errors for the reduction of noise, (ii) modifying the basic algorithm of tooth contact analysis, (iii) stress analysis of the modified face gear drive.

**Keywords:** Transmission errors, Local synthesis, Bearing contact, Tooth contact analysis, Stress analysis.

## INTRODUCTION:

Theory, design, simulation of meshing, generation and stress analysis was the subject of research of many distinguished scientists and leading gear companies. The extended list of references relates the contents of the paper with the basic development of theory of gearing, differential geometry, design and manufacturing of gear drives, and stress analysis.

The contents of this paper cover conceptually the latest developments accomplished by the authors that represent a team of researchers united by the same methodology. The developed approach is based on application of (i) modification of geometry of gears, (ii) application of a modified tooth contact analysis (TCA) algorithm, and (iii) application of an enhanced approach for application of the finite element method to stress analysis [1]. The main topics of the paper are:

### Reduction Of Noise Of Gear Drives:

The reduction of noise is achieved by application of a predesigned parabolic function of transmission errors. Such a function is able to absorb discontinued linear functions of transmission errors with a large magnitude of maximum transmission errors. The discontinued functions of transmission errors are caused by errors of alignment such as change of shaft angle, center distance of some spatial gear drives, errors of machine-tool settings, etc. The advantage of application of a predesigned parabolic function of transmission errors is confirmed by simulation of the noise caused by typical function of transmission errors of misaligned gear drives [5]. This can be achieved ahead of the manufacturing of a designed gear drive.

### Modified TCA Approach:

The proposed modification of TCA is based on an algorithm for determination of guess values for the starting point of tangency of mating surfaces. The guess values may be determined considering only a known at the start of computation the machine-tool settings used for gear generation [1]. Then, it becomes possible to develop a TCA program for simulation of meshing of manufactured gears.

### Enhanced Approach For Application Of FEM To Stress Analysis:

The enhanced approach for application of the finite element method to stress analysis is based on application of a contacting model for mating gears developed by using an analytical representation of tooth surfaces. This allows avoiding codes for the numerical development of the contacting model [2]. The stress analysis is complemented with investigation of formation of the bearing contact and enhanced design of face-gear drives.

The applied enhanced design of gear drives covers:

- (i) Design of low noise spiral bevel gears that is based on application of: (a) combination of local synthesis and TCA; (b) modified roll and modification of geometry of generating tool; (c) an approach for reduction of noise.
- (ii) Basic concepts of design and analysis of face-gear drives, and a new approach for generation of face-gears by grinding and cutting (applying for this purpose a worm of special shape).
- (iii) Modification of geometry of helical gears with parallel axes that is based on:
  - (a) Localization of bearing contact by substitution of line contact of tooth surface by point contact; (b) generation of gears by a plunging disk or by a worm (hob) that enables to reduce the noise and improve the bearing contact;
  - (c) Application of TCA for analysis of misaligned gear drives.

## 2.0 FUNCTIONS OF TRANSMISSION ERRORS:

It has been already recognized by researchers that the main source of noise and vibration are transmission errors. Such errors are caused by misalignment of gear drives such as change of shaft angle, change of center distance (for some spatial gear drives), errors of installment of machine-tool settings, etc [5]. The results of TCA show that the real transmission function of a misaligned gear drive is a piecewise linear function of transmission errors.

The main idea of the authors for the design of gear drives with reduced noise is based on application of a pre-designed parabolic function of transmission errors. A pre-designed parabolic function of transmission errors absorbs linear

functions of transmission errors caused by misalignment and this is the main condition of reduction of noise.

The analysis of meshing may be performed in the following sequence:

- (i) derivation of gear tooth surfaces by using of the basic machine-tool settings applied for surface generation; (ii) approximate determination of a contact point, used as a guess value for TCA; (iii) development of TCA and analysis of meshing.

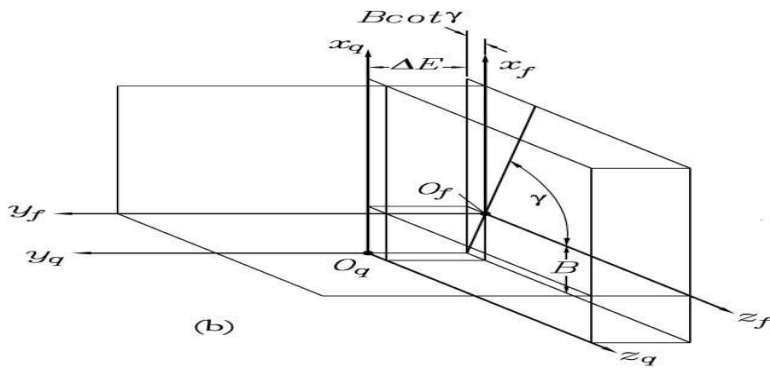
## TOOTH CONTACT ANALYSIS:

### Introductory Remarks

Structure of Face Gear Tooth. The tooth surfaces  $\Sigma_2$  of the face-gear generated by an involute shaper. Lines  $SL_2$  represent the instantaneous lines of tangency of  $\Sigma_2$  and shaper  $\Sigma_1$  shown on  $\Sigma_2$ . Investigation shows that the surface points of the face-gear are hyperbolic ones. This means that the product of principal curvatures at the surface point is negative. The fillet of the face-gear tooth surface of a conventional design is generated by the edge of the shaper  $r$ . The authors have proposed to generate the fillet by a rounded edge of the shaper as shown in Fig. 4 that allows the bending stresses to be reduced approximately in 10%. The shape of the modified fillet of the face gear is shown in Fig. 1. The length of the face-gear teeth has to be limited by dimensions  $L_1$  and  $L_2$ : (i) undercut in plane A, and (ii) tooth pointing in plane B [9]. The permissible length of the face-gear tooth is determined by the unitless coefficient  $c$  represented as  $m$ .

$$C = (L_2 - L_1) P_d = L_2 - L_1 / m$$

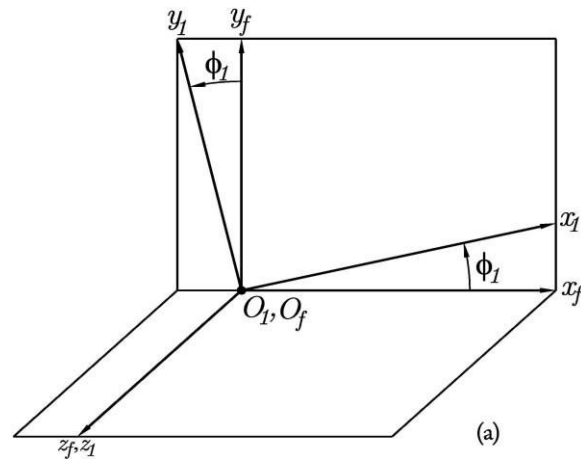
Where  $P_d$  and  $m$  are the diametric pitch and the module, respectively. The magnitude of coefficient  $c$  depends mainly on the gear



**Fig.1**Coordinates systems applied for simulation of meshing:(a)Coordinates systems  $S_q, S_d, S_e$

$M12=N2/N1$  and is usually in the range  $8 < c < 15$ .

Results of TCA (Tooth Contact Analysis): TCA is designated for simulation of meshing and contact of surfaces  $\Sigma 1$  and  $\Sigma 2$  and permits the investigation of the influence of errors of alignment on transmission errors and the shift of bearing contact [9]. The TCA algorithm is based on observation of continuous tangency of pinion and face-gear tooth surfaces  $\Sigma 1$  and  $\Sigma 2$ . Application of the TCA program indicates: (i) errors of alignment do not cause transmission errors, but (ii) cause the shift of bearing contact. The advantage of zero transmission errors is the result of application of an involute pinion that has equidistant profiles. The sensitivity of the bearing contact of the face gear drive to errors of alignment requires special corrections to obtain a central location of the bearing contact. It has been proven that this can be obtained by axial displacement  $\Delta q$  of the face-gear with respect to the pinion. The investigation is based on application of coordinate systems. Coordinate systems  $S_1$  and  $S_f$  are rigidly connected to the pinion and the frame of the face-gear drive, respectively [19]. To simulate the misalignment of the face-gear, we use auxiliary coordinate systems  $S_q, S_d$  and  $S_e$ . The location of  $q$   $S$  with respect to  $f$   $S$  is Parameters  $\Delta E, B$  and Both determine the location of the origin  $O_q$  with respect to  $O_f$ . Here,  $\Delta E$  is the shortest distance between the pinion and the face-gear axes when the axes are crossed but not intersected.



**Fig.2**Coordinates systems applied for simulation of meshing:Coordinate Systems  $S_2, S_e$

Auxiliary fixed coordinate systems  $S_q, S_d$  and  $S_e$  are shown. The face-gear performs rotation about the  $z$  axis. The location of  $S_e$  with respect to  $S_d$  simulates the axial displacement  $\Delta q$  of the face-gear (Fig 2).

## ENHANCED APPROACH FOR STRESS ANALYSIS

### Application Of The Finite Element Analysis (FEA) Enables:

- (1) Determination of contact and bending stresses for the pinion and the gear.
- (2) Investigation of formation of bearing contact taking into account that the meshing is transferred from one pair of teeth to the neighboring one.
- (3) Detection and avoidance of areas of severe contact stresses.

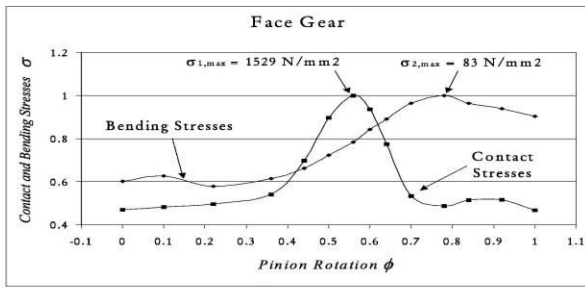
Application of the finite element method requires the development of the finite element model formed by the finite element mesh, the definition of contacting surfaces, and the establishment of boundary conditions to load the gear drive with the desired torque. The authors apply a general purpose computer program to perform the finite element analysis. An enhanced approach for application of finite element analysis has been used for design of gear drives. One of the main ideas of the applied FEA approach is the auto-immunization or derivation of the contacting model of gear teeth by direct application of tooth surface equations [7]. This approach enables to determine contact and bending stresses for the whole cycle of meshing, investigate the formation of the bearing contact and determine, if they exist, hidden areas of severe contact wherein the contact stresses are substantially increased.

## 5.0 DESIGN OF FACE GEAR DRIVES:

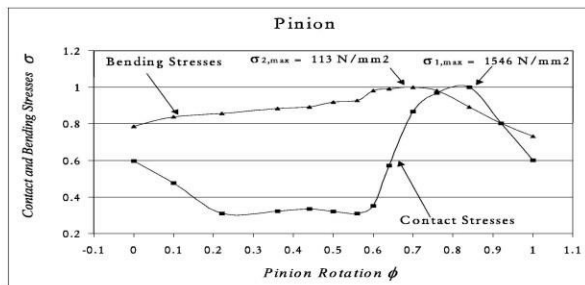
### 5.1. Introduction

A face gear drive is formed by a spur or helical gear and a conjugated gear with tooth located on the gear "face"

(Figure 13). The manufacturing of face gear drives based on application of a shaper has been invented by the Fellows Corporation. The shaper is identical to the pinion of the drive, but the number of shaper teeth is increased in comparison with the pinion teeth for the purpose of localization of bearing contact [5]. The contributions to the design, simulation of meshing, stress analysis, and manufacturing of face-gear drives. The contents of this section cover: (i) development of new geometry of face-gears, and (ii) generation of face-gears by grinding or cutting (by application of a tool similar to a worm of a special shape). Results of TCA for tooth driving side for previous design: (a) and (b) contact pattern and contact path on the gear and pinion tooth surfaces, respectively; (c) function of transmission errors (Fig. 3).



(a)



(b)

**Fig3: Variation of functions of contact and bending stresses during the cycle of meshing for (a) the face-gear and (b) the pinion**

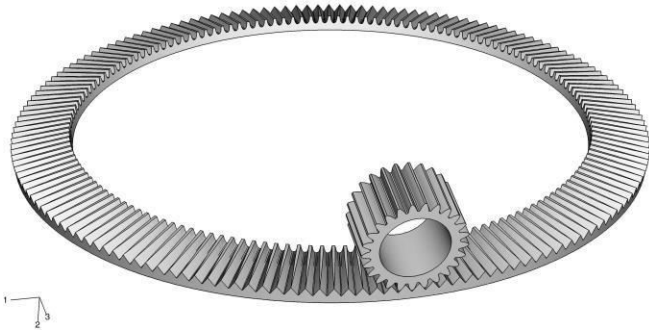
### Generation of Face-Gear By A Shaper

For the purpose of localization of contact and even avoidance of separation of pinion and face-gear tooth surface (in a misaligned gear drive), the tooth number  $N_s$  of the shaper is larger than the tooth number  $N_p$  of pinion teeth, where  $N_s - N_p = 2/3$ .

### 5.3. Conventional Design of Face-Gear Drives

The conventional design of face-gear drives is based on application of involute profiles of the pinion and the shaper. [6] The limitations of such design are:

- (i) Appearance of singularities of tooth surface of the face-gear (it is the herald of the oncoming undercutting of the face-gear).
- (ii) Pointing of face-gear teeth.
- (iii) Limitation of parameters  $L_1$  and  $L_2$  to avoid undercutting and pointing, respectively (Fig 4).



**Fig4:Illustration of Whole gear drivemodell**

(iv) Results of TCA show that: (1) the path of contact is directed across the tooth surface, and (2) errors of alignment may cause the shift of the bearing contact and even edge contact.

(v) The advantage of application of involute profiles for the shaper and the pinion is that errors of alignment do not cause transmission errors. A new version of geometry of face-gear drives has been recently developed that enables to obtain a longitudinal bearing contact. A parabolic function of transmission errors of limited magnitude has to be provided for a misaligned gear drive. The new version of geometry is based on application of profiles (of pinion and shaper) that are conjugated to parabolic profiles of imaginary parabolic rack-cutters [7].  $S_b$  and  $S_c$  are applied for illustration for installment of the worm with respect to the shaper. Axes  $z_s$  and  $z_w$  are the axes of rotation of the shaper and the worm, respectively, and they form a crossing angle of  $90^\circ$ . The upper (and lower) sign correspond to application of a right-hand (left-hand) worm.

## 6.0 CONCLUSION:

Based on the results of the performed research, the following conclusions may be drawn:

- (1) Application of a pre-designed parabolic function of transmission errors enables to reduce the noise and vibration. This statement is confirmed by computerization of noise of a misaligned gear drive.
- (2) Effective methods of development of TCA have been developed.
- (3) Enhanced approaches for computerized design, simulation of meshing, and stress analysis have been developed for face-gear drives

## 7.0 REFERENCES:

- [1] Argyris, J., Fuentes, A. and Litvin, F.L., ‘Computerized integrated approach for design and stress analysis of spiral bevel gears’, *Comput. Methods Appl. Mech. Eng.* 191 (2002)1057–1095.
- [2] Fuentes, A., Litvin, F.L., Mullins, B.R., Woods, R., Handschuh, R.F. and Lewicki, D.G., ‘Design, stress analysis and experimental tests of low-noise adjusted bearing contact spiral bevel gears’, in: *Proceedings International Conference on Gears, VDI-Berichte, Vol.1, No.1665, (2002)327–340.*
- [3] Litvin, F.L., *Theory of Gearing, NASARP-1212 (AVSCOM 88-C-C035), Washington, D.C., 1989. Computerized Developments 323*
- [4] Litvin, F.L., *Development of Gear Technology and Theory of Gearing, NASA Reference Publication 1406, ARL-TR-1500, 1998.*
- [5] Litvin, F.L., Fuentes, A., Zanzi, C. and Pontiggia, M., ‘Design, generation, and stress analysis of two versions of geometry of face-gear drives’, *Mech. Mach. Theo.* 37 (2002)1179–1211.
- [6] Litvin, F.L., Fuentes, A., Zanzi, C., Pontiggia, M. and Handschuh, R.F., ‘Face gear drive with spur involute pinion: geometry, generation by a worm, stress analysis’, *Comput. Methods Appl. Mech. Eng.* 191(2002)2785–2813.
- [7] Litvin, F.L., Fuentes, A., Gonzalez-Perez, I., Carnevali, L. and Sep, T.M., ‘New version of Novikov-Wildhaber helical gears: Computerized design, simulation of meshing and stress analysis’, *Comput. Methods Appl. Mech. Eng.* 191(2002)5707–5740.
- [8] Litvin, F.L., Fuentes, A., Gonzalez-Perez, I., Carnevali, L., Kawasaki, K. and Handschuh, R.F., ‘Modified involute helical gears: computerized design, simulation of meshing, and stress analysis’, *Comput. Methods Appl. Mech. Eng.* 192(2003)3619–3655.
- [9] Litvin, F.L., Sheveleva, G.I., Vecchiato, D., Gonzalez-Perez, I. and Fuentes, A., ‘Modified approach for tooth contact analysis of gear drives and automatic determination of guess values’, *Comput. Methods Appl. Mech. Eng.*, accepted for publication, (2004).
- [10] Medvedev, V.I. and Sheveleva, G.I., ‘Synthesis of bevel gearings on the basis of the theory of quasilinear contact’, *J. Mach., Manufacture and Reliability* 2(1996)18–24.
- [11] Faydor L. Litvin, Alfonso Fuentes, Claudio Zanzi, and Matteo Pontiggia University of Illinois at Chicago, *Face Gear Drive With Spur In volute Pinion: Geometry, Generation by a Worm, Stress Analysis, NASA/CR—2002-211362 February 2002.*
- [12] Shyue-Cheng Yang, *Mathematical model of a helical gear with asymmetric involute teeth and its analysis*, © Springer-Verlag London Limited, 10 November 2003.
- [13] Goutam Pohit, *Application of virtual manufacturing in generation of gears.* # Springer-Verlag London Limited. Published online: 24 November 2005
- [14] Grzegorz Litak and Michael I Friswell, *Dynamics of a Gear System with Faults in Meshing Stiffness* # Springer 2005.
- [15] Saeed Ebrahimi · Peter Eberhard *Rigid-elastic modeling of meshing gear wheels in multibody systems: C Springer Science+Business Media B.V. 3 May 2006*
- [16] Piermaria Davoli, Carlo Gorla, Francesco Rosa,



Fabrizio Rossi and Giuseppe Boni, Transmission Error and Noise Emission of Spur Gears., March/April 2007.

[17] Peter Ward and Sheree Hindmarsh An overview of historical changes in the fishing gear and practices of pelagic long liners, with particular reference to Japan's Pacific fleet, Springer Science+ Business Media B.V. 11 April 2007.

[18] Bernd-Robert Hohn and Klaus Michaelis and Hans-Philipp Otto, Influence of immersion depth of dip lubricated gears on power loss, bulk temperature and scuffing load carrying capacity, Springer Science+Business Media B.V. 14 August 2007