

# Dynamic Model Analysis for Unsteady Operating of Double V-Belt Drive System

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## Abstract

Alignment issues of the transmission V-belt drive system using numerical model are one of the challenges we are trying to find ways to deal with them. Experiments and dynamic model analysis were performed to monitor and predict of alignment issues of the transmission system. Various types of transmission system misalignment were investigated using the developed model. Using different two statistical parameters, RMS and Crest factor, the vibration level was monitored. The results obtained during the study confirmed that you have a type each type of alignment issues has an optimal way to deal with it in terms of locating the appropriate position to install the sensor. Moreover, the results display that it can use the RMS and CF statistical parameters of the acceleration responses to detect and monitor of the transmission system misalignment. Furthermore, the mathematical model may be considered as an alternative method to detect vibration signals of the transmission system using the spring-mass system.

**Keywords:** Dynamic model, misalignment, V-belt, mathematical model and vibration analysis.

## Introduction

Vibration measurements and significant analyzes for transmission belt drive systems play a vital role in malfunction detection. The fault monitoring system helps to reduce downtime and prevent consequential failure, which reduces economic losses. Belt drive System generate a regular impulse during healthy condition, while the fault can be identified via note a significant signals change. Therefore, vibration analysis is usually an effective method to detect faults that facilitate maintenance and allow to be scheduled. An intelligent method is applied to detect faults in the tolerance of excitatory motors inspired by the artificial neural networks. The results showed a clear improvement due to filter the vibration signal component comparing with the traditional methods that use the vibration signal directly. The new method has proven its efficiency in detecting faults even with low-frequency vibrations [1]. Vibration analysis is widely used as one of the most important maintenance methods used to treat with the malfunctions of various machine parts. This has led to an increase in the urgent need for development and the search for clear approaches to display the system oscillation [2,3]. New model based on time dependent

displacement excitation is performed as a tool to obtain the vibration excitations of the bearing faults. The localized faults on the outer race with three different cases, parallel, bias and offset, is investigated. The contact stiffness parameter of the bearing is calculated using the Hertzian contact theory. A comparative study was done between the three different faults cases. Based on the results obtained, the model is considered a new approach to enhance and analyze the study of vibrations more precisely [4]. Envelope analysis and Duffing oscillator is adopted to study the deep groove ball bearing with local faults presence on the races. The test rig is equipped to test the defected bearings via vibration sensors. The conclusion of this work is focused on the fact that the envelope analysis displays the vibration profile with a distinct frequency and identify bandwidth [5]. Based on Hamilton's principle, a flat belt drive model is created according to nonlinear dynamic assumption. While the model controls the stationary operation and corresponds with elastic-plastic contacts, which neglects the adhesion areas. From the previous results, the stability analysis is possible to evidences that solutions with a nonlinear dynamic assumption are suitable method [6]. A statistical analysis method is utilized to study vibration impacts [7-10]. Therefore, the analytical method is performed to record the vibration responses via the frequency band [11]. The defects size presence on the outer race of the tapered roller bearing is developed using the numerical model [12].

The belt pulley system malfunctions such as unbalance, misalignment and belt worm were diagnosed using frequency band by FFT [13, 14]. Statistical parameters of vibration responses for healthy and unhealthy component were compared [15]. The oscillation amplitude of the belt drive system is shown to monitor the friction and rotation instability parameters under different conditions of loading and speed [16]. The friction of the belt pulley is an obstacle to ensuring efficient power transmission. The V-shaped metal belt model was verified to estimate torque loss due to rubbing forces and the losses of the pulley deflection [17]. A belt transmission model is established as a set of elements links, springs and dampers are connected each other in two-dimensional scale under assumptions of free transition and rotational stiffness [18]. Whilst in situations of multi transmission system, the problem is to find a way to define the number of points appropriate to achieve the required precision of belt bending around the individual pulleys. The mapped points make it easier to use as illustrative markers to study the oscillation of the transmission system [19]. A belt pulley drive system under steady-state operating transient is investigated using the finite element analysis. The contact area between the belt and pulley are determined using a penal formula with rubbing contact according to Coulomb's triple linear law of friction. Also, the drive pulley is designed in the form of circular restraints that rotate at a certain angular speed [20]. The simulated vibration pattern and experimental results have the same results characteristics [21]. The unstable belt moving process was studied assuming that the forces applied on the stick-slip regions are the same via the perturbation solution. By checking the perturbation and numerical solutions, it was observed that the results showed an acceptable agreement [22]. A dynamic model of transmission belt drive system with different damaged cases was performed to evaluate the vibration responses. Different damaged cases as missing cogs, and belt alignment issues with different angles are diagnosis using statistical parameters [23-

24].Moreover, a new attempt to studythe pulleydurability was achieved by creating a model using a commercial software package ABAQUS.Comparing numerical and experimental results, there is a close convergence[25].

### Experimental Setup

Figure 1shows the details of the device used to conduct the experiments.PT 500 (GUNT Hamburg) Machinery diagnostic system unit is used to investigate conditions that cause vibration or unsteady operating conditions.The experimental vibration signals are measured by analog accelerometers device, PCB manufactures sensors, used to record vibration data.The signals detected through from amplifier to the data acquisition card (BMC USB-AD16F) to measure and evaluate the vibration signals. The rotating speed of the belt is estimated using diffuse photoelectric sensor, Baumer.To analysis of the vibration signals, the software is used to record the vibration displacement and acceleration in the time/frequency spectrum.The belt kit is a double pulley with a roller belt tensioner for both V-belts. The pulleys are assembled using clamping sets. The experiments also include a V-belt with defect and an eccentrically small belt pulley.The vibration responses for a belt drive system is to be recorded with a different drive speeds and applied loads.

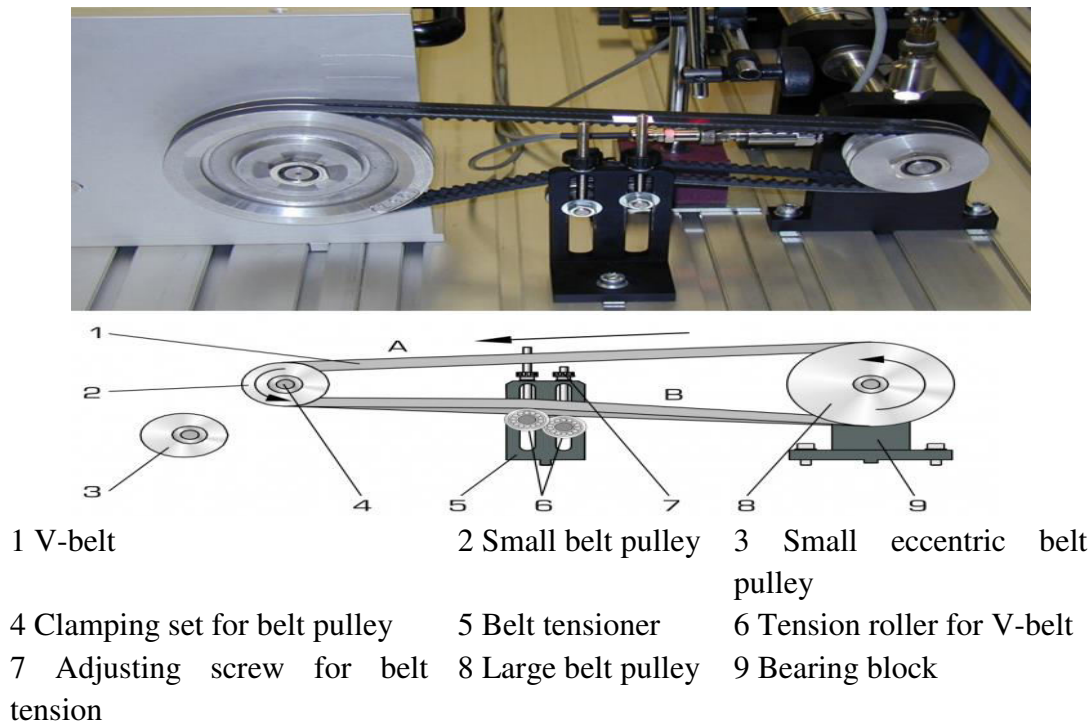


Figure 1. Double V-belt pulley test rig.

### Numerical Model Creation

The model creation is performed in Abaqus/Explicit to simulate double V-belt drive system and to carry out casestudies for various unsteady operating parameters.A three-dimensional model is required to predict the vibration oscillation and monitor the systemmalfunction. The analysis is run in many stepsto accomplish this model.The 3D model ofthe transmission system was created with SolidWorks and then imported into an Abaqus/CAE package. Thebelt material is PUrubber,

which properties were listed as 70 MPa of modulus of elasticity, poisson's ratio is 0.4 and density is  $1200 \text{ kg/m}^3$ . While the material of pulleys system is a cast iron, which properties were listed as  $67 \times 10^3 \text{ MPa}$  of modulus of elasticity, poisson's ratio is 0.33 and density is  $2705 \text{ kg/m}^3$ . The transmission system analysis is run depending keeping the pulley with no movement allowed, Zero degree of freedom - Encastre, and in the other pulley is accelerated, one degree of freedom, with angular velocity about Z-coordinate VR3. The interaction between pulleys and belt can be obtained using smooth step option. 8-nodes brick elements with reduced integration were performed to mesh the model.

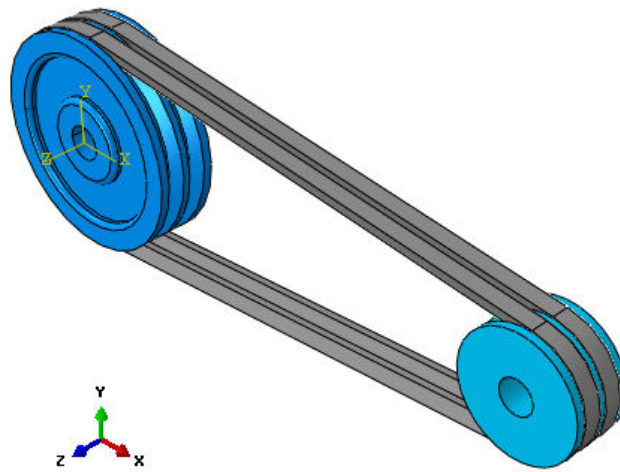


Figure 2. Schematic structure of Double V-belt pulley

### ***The Mathematical Model of the System***

The analysis of transmission system can be obtained by considering the spring-mass system. This system consists of a V-belt resting over two pulleys, a driver and a driven pulley, and power source, a motor. The tension roller is pressing against the V-belt in such a way that it can be used to increase the tension force. Figure 3 illustrates a spring-mass system that displays the simplest possible oscillation transmission system. Develop a sequence of mathematical model of the system for investigating vibration response of this system. Consider the elasticity of the belt can be analyzed by massless linear spring, while the driver and driven pulleys rotate by an  $\theta_{DR}, \theta_{DN}$  angles and rotational masses  $J_{DR}, J_{DN}$ , respectively. The motor of rotational mass  $J_m$  is rotated by an angle  $\theta_{DR}$  as a result of the coupling of the motor and the driver pulley. Also, considering that the mass  $M_o$  is equivalent to the forces resulting from tension roller.

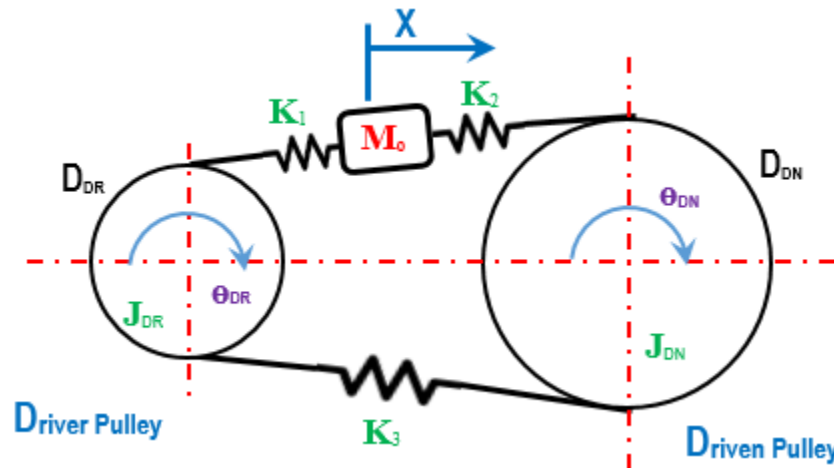


Figure 3.A spring-mass system of the belt drive.

The analytical solution of this transmission equipment can be performed by applying of Newton’s second law of motion [26-27]:

$$(J_{DR} + J_M)\ddot{\theta}_{DR} = R_{DR}^2 K_1(X)\theta_{DR} - R_{DR}K_1(X)X - R_{DN}^2 K_3\theta_{DN} + R_{DN}K_3R_{DR}\theta_{DR} \quad [1]$$

$$J_{DN}\ddot{\theta}_{DN} = R_{DN} [K_2(X)X - R_{DN}K_2(X)\theta_{DN} - R_{DN}K_3\theta_{DN} + R_{DR}K_3\theta_{DR}] \quad [2]$$

$$M_o\ddot{X} = K_1(X)R_{DR}\theta_{DR} - K_1(X)X + K_2(X)R_{DN}\theta_{DN} - K_2(X)X \quad [3]$$

Boundary conditions can also be applied of this equipment to cases of friction. Both of the contact friction on the belt-pulley region and the friction concentrated in the contact area of the tension roller may be taken into account. In the present, the friction will be performed, so a mathematical solution of this equipment can be estimated by as follows:

$$(J_{DR} + J_M)\ddot{\theta}_{DR} + f_{DR} = R_{DR}^2 K_1(X)\theta_{DR} - R_{DR}K_1(X)X - R_{DN}^2 K_3\theta_{DN} + R_{DN}K_3R_{DR}\theta_{DR} \quad [4]$$

$$J_{DN}\ddot{\theta}_{DN} + f_{DN} = R_{DN} [K_2(X)X - R_{DN}K_2(X)\theta_{DN} - R_{DN}K_3\theta_{DN} + R_{DR}K_3\theta_{DR}] \quad [5]$$

$$M_o\ddot{X} + f_o = K_1(X)R_{DR}\theta_{DR} - K_1(X)X + K_2(X)R_{DN}\theta_{DN} - K_2(X)X \quad [6]$$

Where

- $J_M$  Inertia moment of the motor;
- $J_{DR}, J_{DN}$  Moment of Inertia of the driving and the driven pulley, respectively;
- $R_{DR}, R_{DN}$  Radius of the driving and the driven pulley, respectively;
- $\theta_{DR}, \theta_{DN}$  Angular position of the driving and the driven pulley, respectively;
- $K_1, K_2, K_3$  Stiffness dependent elasticity coefficients of the belt;
- $M_o$  Tension roller loading on the belt;
- $X$  Belt elongation position;
- $f_{DR}, f_{DN}$  Friction torque of the driving and the driven pulley, respectively;
- $f_o$  Friction force of the tension roller

## Results and Discussion

### 1. Validation Between Experimental and Numerical Model

The experiments and the numerical model are examined under same operating conditions. The vibrationsignals are to be recorded for a belt drive with the parameters of pretension of the belt 130 N and shaft speed of 2500 rpm.The vibration signalsare recorded using a vertical accelerometer device. The belt speed is recorded using diffuse reflectiondevice.From the Figure 4, it is possible to see how the drive shaft speed has only meaningful effect on the vibration profile for undamaged belts where speed should result in fundamental frequency values  $f_{D1}$ in Hz and its harmonic of drive speed  $f_{D2}$ .In contrast,the vibration profile for damaged beltcan clearly be seen the Belt vibration frequency $f_{R1}$ (8.8 Hz) and the harmonics  $f_{R2...Rn}$ of the belt frequency.Frequency of the belt can be calculated using the formula;

$$f_R = (N \times C_{DR}) / (60 \times L_b) \tag{7}$$

Where, N is driver speed in rpm,  $L_b$ is V-belt length and  $C_{DR}$  is circumference of the driver pulley. The boundary conditions of the numerical solutionhave been applied to fit the experimental set up.It can notice form the Figures 4-7 that the numerical results have approximately the same trend of the experiment results.According to the results, it can be concluded that the numerical solution can be used as a reliable method through which various malfunction can be identified and vibration responses for each case becomes available.

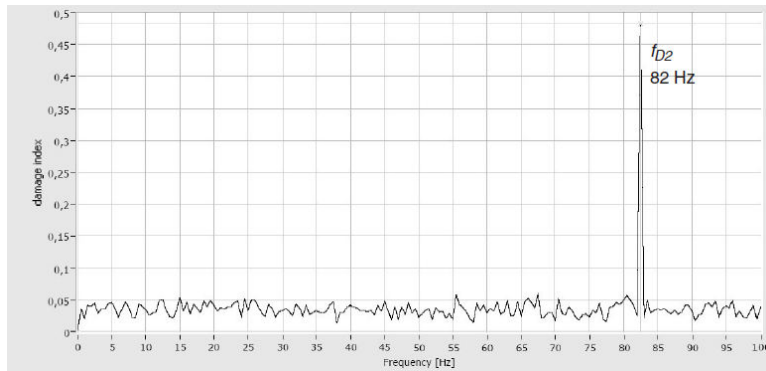


Figure 4. Vibration response for the undamaged V-belt using envelope analysis

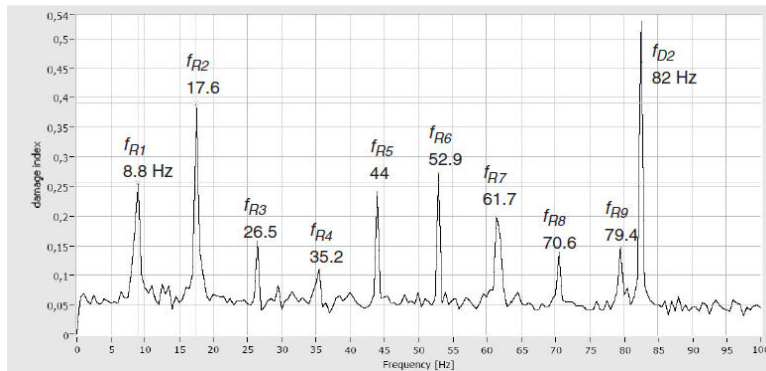


Figure 5. Vibration response for the damaged V-belt using envelope analysis

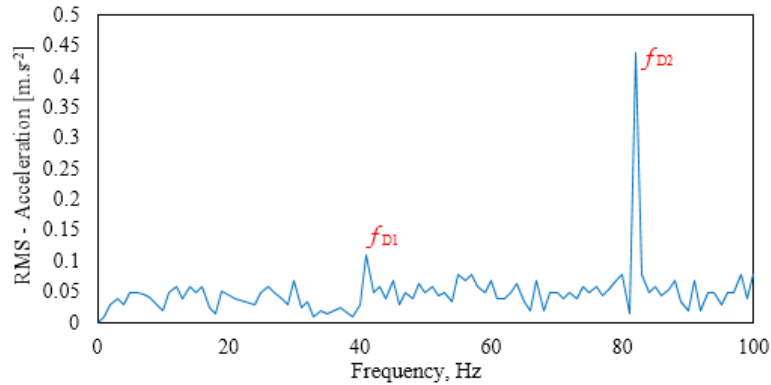


Figure 6. Vibration response for the undamaged V-belt using Numerical Model

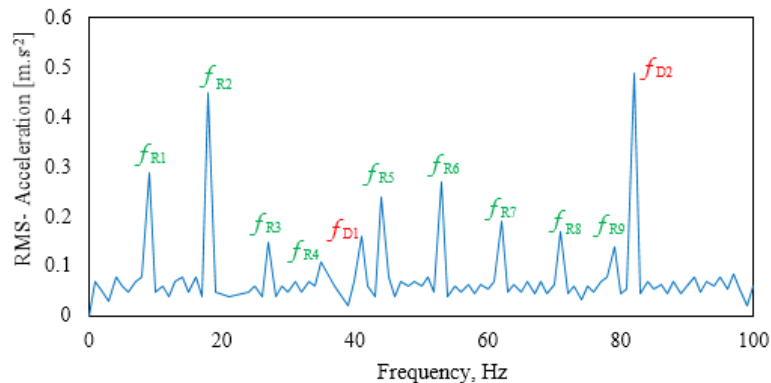


Figure 7. Vibration response for the damaged V-belt using Numerical Model

## 2. Transmission Drive System Alignment

Aligning the transmission belt drive system is an important maintenance task as is shaft alignment. The belt drive system alignment is also related to the friction between the belt and the pulley, which leads to increase the belt wear and loss of the motor power. There are various types of belt misalignment as illustrated in Figure 8. In practice, any error in the installation can cause of different misalignments is often encountered simultaneously. Previous validation proved that the numerical model can predict the vibration characteristics of the transmission system under different operating conditions. The analysis of system results may be performed by recording vibration data of the standard operating belt as a reference case to identify the signals changes of various types of belt alignment issues. The statistical analysis, RMS, and CF, is applied to monitor and control the vibration and noise level of the transmission system, which in turn shortens the belt's life. The acceleration signals were measured in both perpendicular directions, horizontal [H] and vertical [V] for the co-ordinates [XYZ]. RMA and Crest factor parameters ratio, is calculated ratio of the magnitude of the damaged to the undamaged vibration values.

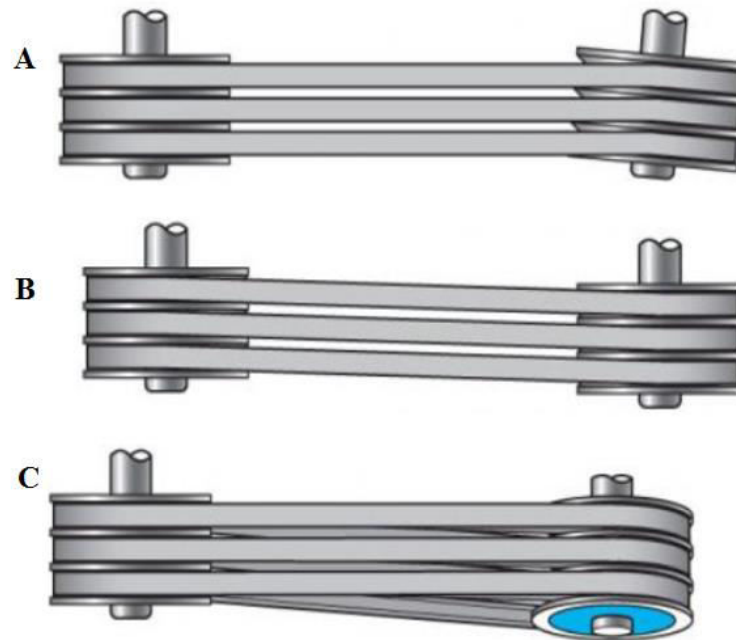


Figure 8. The three different types of transmission belt drive system misalignment (A) horizontal angle misalignment, (B) parallel misalignment, and (C) vertical angle misalignment.

### 2.1 Parallel Misalignment

The offset alignment of the transmission belt drive system is one of the recurring issues when installing and maintaining these systems. The numerical model was performed to calibrate this case study. A parallel misalignment of 0.5, 1.0, 1.5, 2.0 and 2.5 mm was considered under a fundamental speed value 2500 rpm [41.67 Hz] and a pretension of the belt 130 N. Figures 9 and 10 show the frequency response of the numerical signals under the aforementioned operating conditions. As shown in Figure 9, the results show that the acceleration ratio RMS values of the numerical signals are regular and are very clear to enable and facilitate the monitoring and detection of the offset alignment of the transmission belt drive system. Nevertheless, it can be noticed that the acceleration characteristic value recorded via the vertical set point is preferable compared to the signal recorded from the horizontal point. In addition, the RMS ratio collected via the vertical set point gives a high result in Y- and Z-coordinates,  $[A_2]$  and  $[A_3]$  respectively. The same observation is valid for the acceleration ratio CF values. However, the acceleration ratio CF recorded via the vertical set point for X- and Z-coordinates,  $[A_1]$  and  $[A_3]$  respectively, as illustrated in Figure 10. On the other hand, the acceleration ratio CF is distinguished more sensitivity to the values of vibration response for minor misalignment cases. It can be concluded that the sensor installed in the vertical position is appropriate for recording system malfunctions with using of the statistical parameters RMS and CF. While, that the horizontal position is not preferred to discover system malfunctions, this is a result of the vibration signals for both damaged and undamaged belt system is approximately the same.



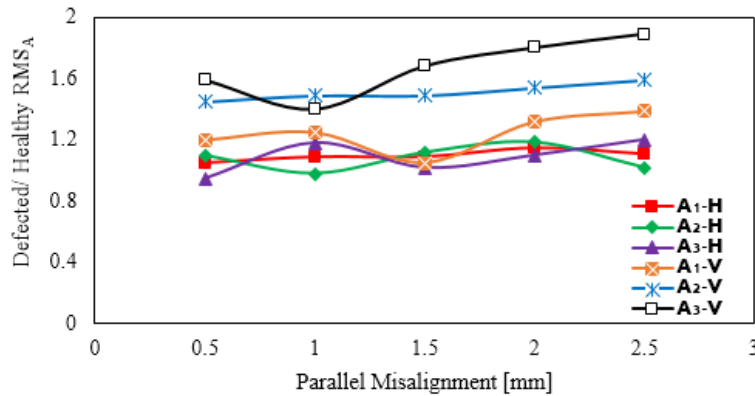


Figure 9. Acceleration ratio RMS of transmission parallel misalignment

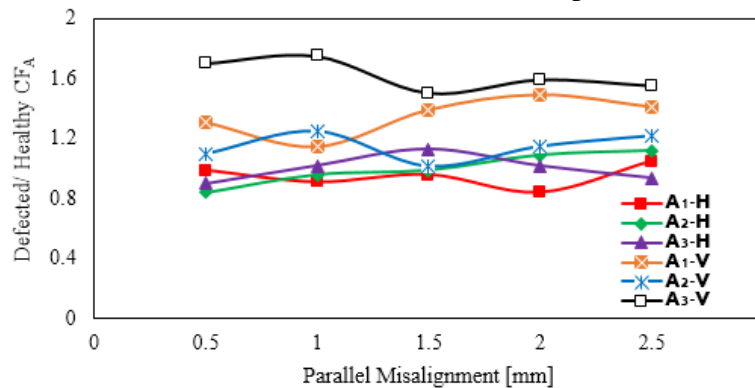


Figure 10. Acceleration ratio Crest Factor of transmission parallel misalignment

### 2.2 Horizontal Angle Misalignment

Horizontal angle misalignment has been investigated via the three-dimensional modeling, where the system misaligns with angles of 0.5°, 1.0°, 1.5°, 2.0° and 2.5°. Figure 101 shows the variation of the acceleration ratio RMS versus different misalignment angles. It can be noticed that, the acceleration signals collected via vertical set point less than that than was recorded for the aforementioned case. On the other hand, it is clearly evident that the horizontal point is an ideal position to detect and monitor this type of misalignment. This phenomenon can be related to the increase of the contact area between the belt and the pulley groove. Nevertheless, it can be predicted that, the probability of wear occurrence increases with the increase of the frictional area. Therefore, Fig. 12 illustrates the relationship between acceleration ratio CF versus different misalignment angles. The respective acceleration ratio CF can be observed for horizontal set point. The results show that, with an increase of the additional load, the vibration amplitude of the RMS acceleration signals coincides comparatively with the acceleration amplitude using CF parameter.

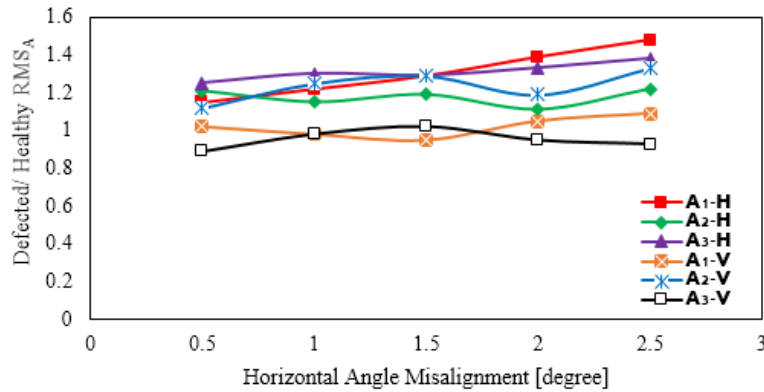


Figure 11. Acceleration ratio RMS of transmission horizontal angle misalignment

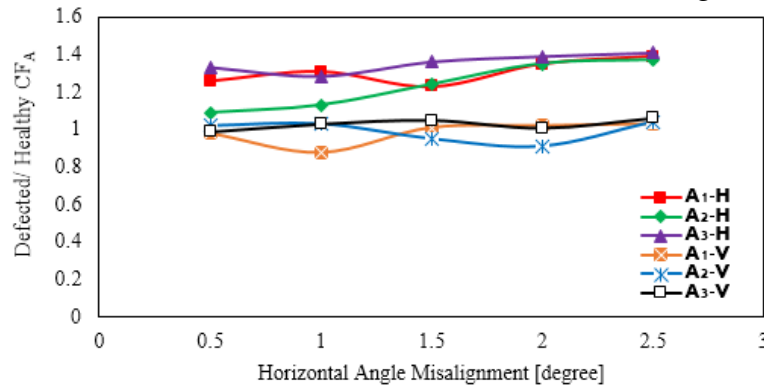


Figure 12. Acceleration ratio Crest Factor of transmission horizontal angle misalignment

### 2.3 Vertical Angle Misalignment

The model is prepared to verify the last casestudy, which is the vertical angle misalignment. Where the transmission system misaligns with vertical angles of 0.5°, 1.0°, 1.5°, 2.0° and 2.5°. The dynamic model results present the monitoring of the acceleration ratio RMS of the vibration response for the transmission system with different vertical misalignment angles, as shown in Figure 13. It can be listed that the value RMS ratio at the horizontal and the vertical set points are greater than 1, that means both positions are suitable to monitor the system malfunctions in this case. It can also be noted a relative advantage of the data collected from the vertical set point over the horizontal one. From Figure 14 it is possible to verify that the same results are achieved again using acceleration ratio CF.

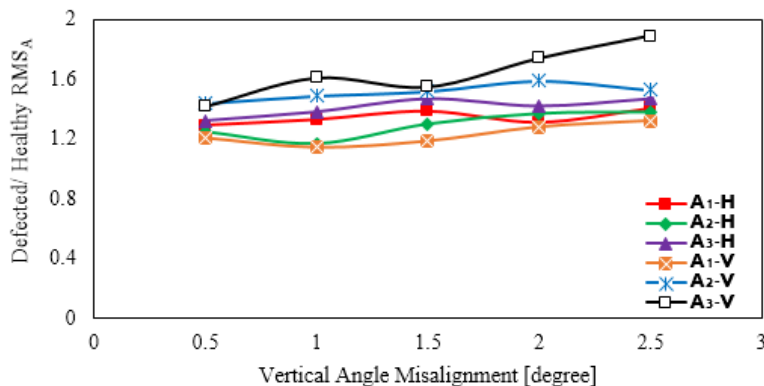


Figure 13. Acceleration ratio RMS of transmission vertical angle misalignment

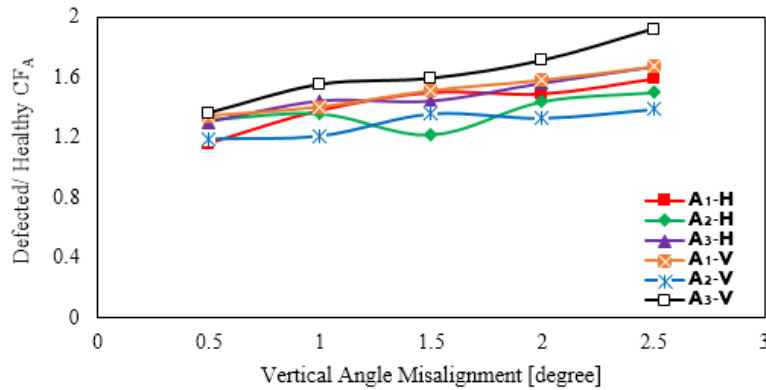


Figure 14. Acceleration ratio Crest Factor of transmission vertical angle misalignment

### 3. The Mathematical Model Analysis

The mathematical model indicates an alternative method to study vibration behavior for the transmission system. In Figure 15 the time domain of the system position is displayed. It can be noticed that the system presents much more oscillatory than steady state case. The accelerations time domain of the two pulleys can be illustrated in Figure 16. It can be seen from that for the acceleration responses of the pulleys are not possible to evaluate the change in this system. Future work includes that, the model may be developed by increase the assumption that helps to present a good prediction and control of the vibration responses of the system using one of the commercial packages.

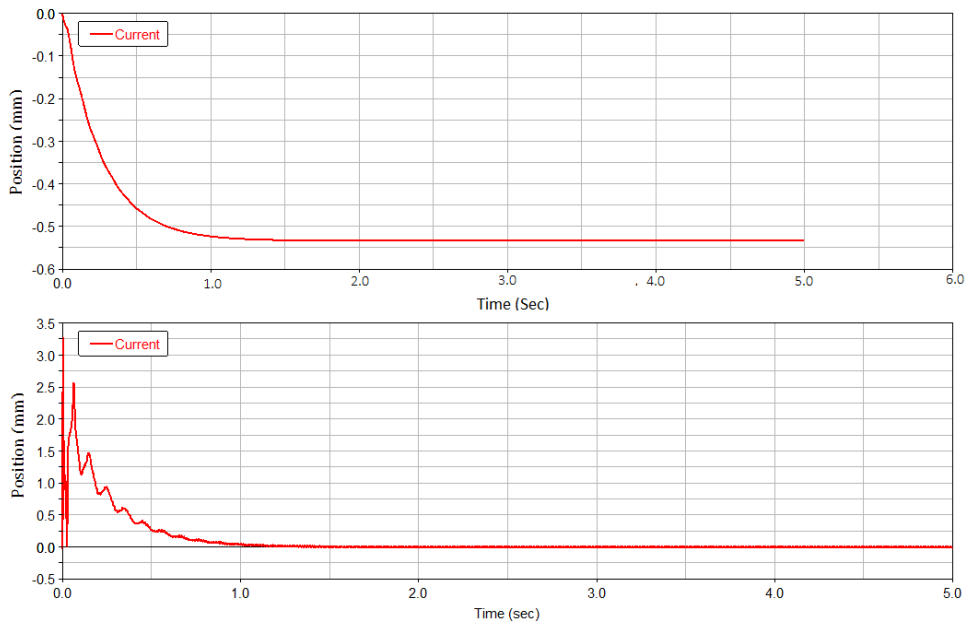


Figure 15. Time responses of system position

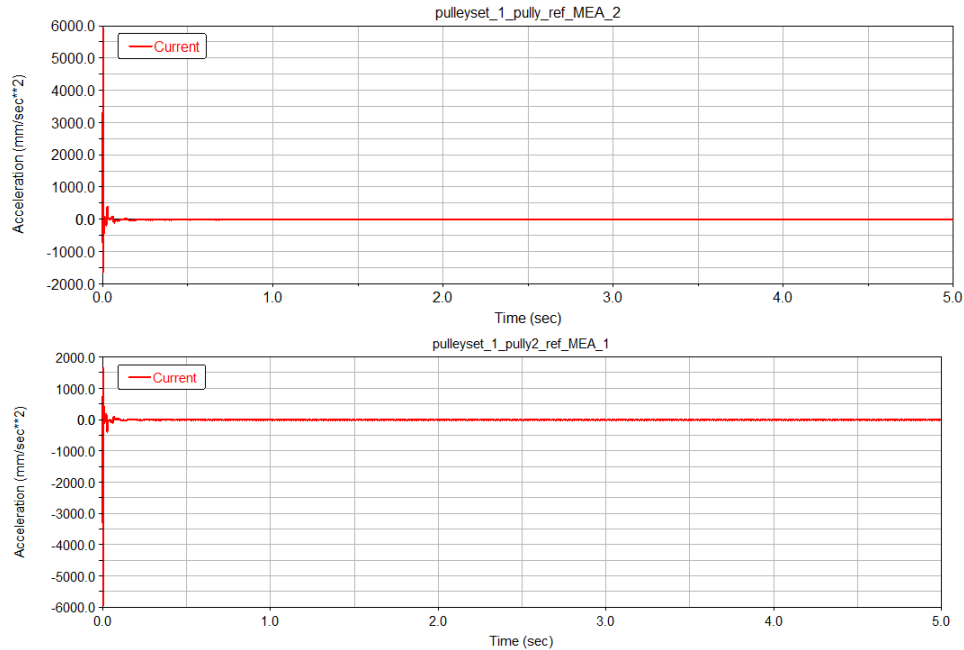


Figure 16. Time responses of system angular acceleration

### Conclusions

The aim of this work is to present a solution based on finite element analysis for aligning the transmission belt drive system using vibration responses. Numerical model of transmission belt drive system is established and vibration behavior monitored using a commercial software package ABAQUS/CAE. Both results obtained by numerical model and the experimental showed a significant agreement. Based on the results, it can be found that the numerical model can be performed to detect and monitor the transmission belt system. By studying different alignment issues, it has been verified that both RMS and Crest Factor parameters are compatible methods to monitor and detect various conditions. For the parallel misalignment, it is listed that the vibration signals are distinguished to receive data via vertical attach point. While the set point must be installed horizontally to detect the system malfunction with horizontal angle misalignment. Moreover, it has been found that RMS and CF parameters can be considered as good points for collecting signals in both directions for vertical angle alignment cases.

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